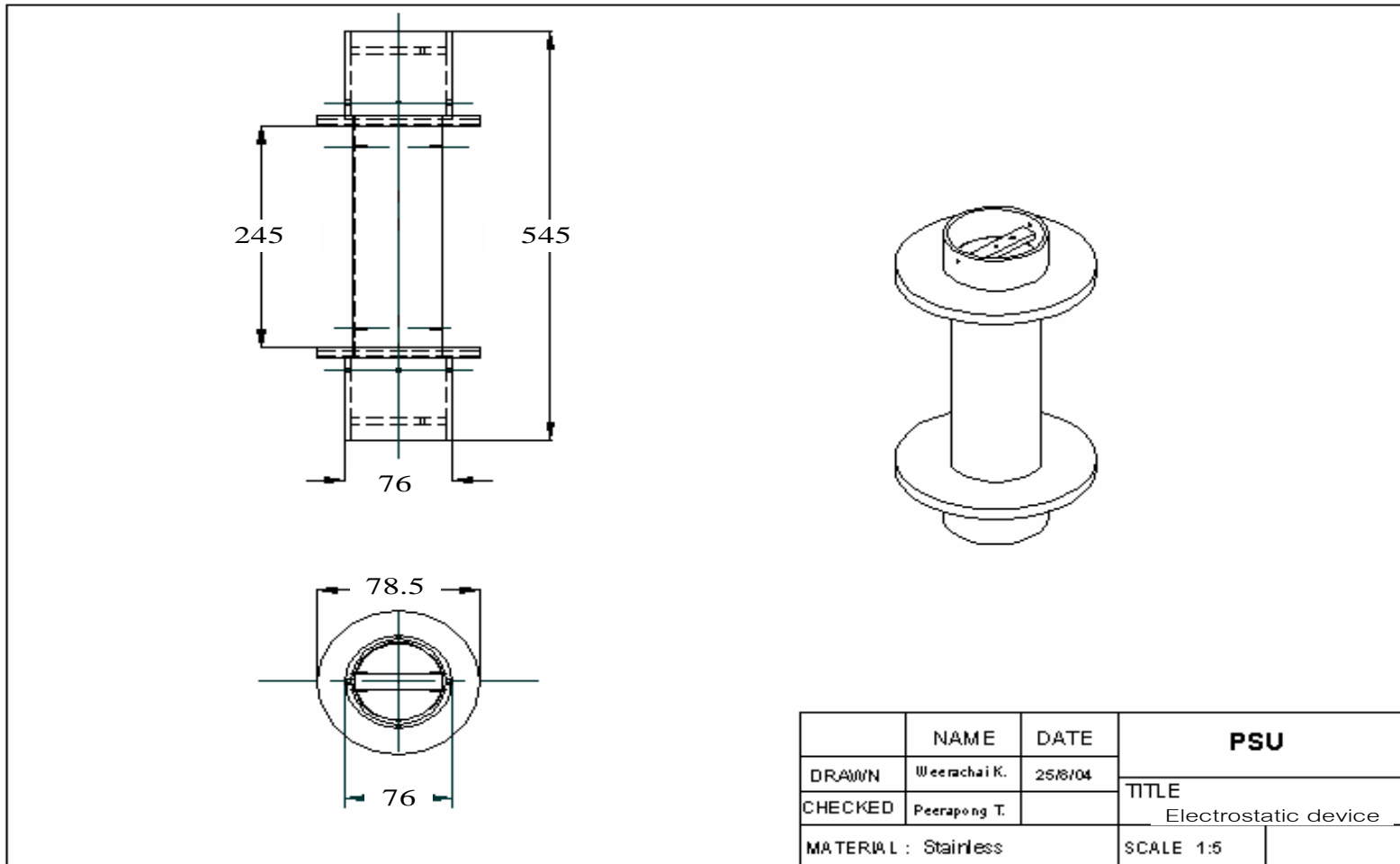
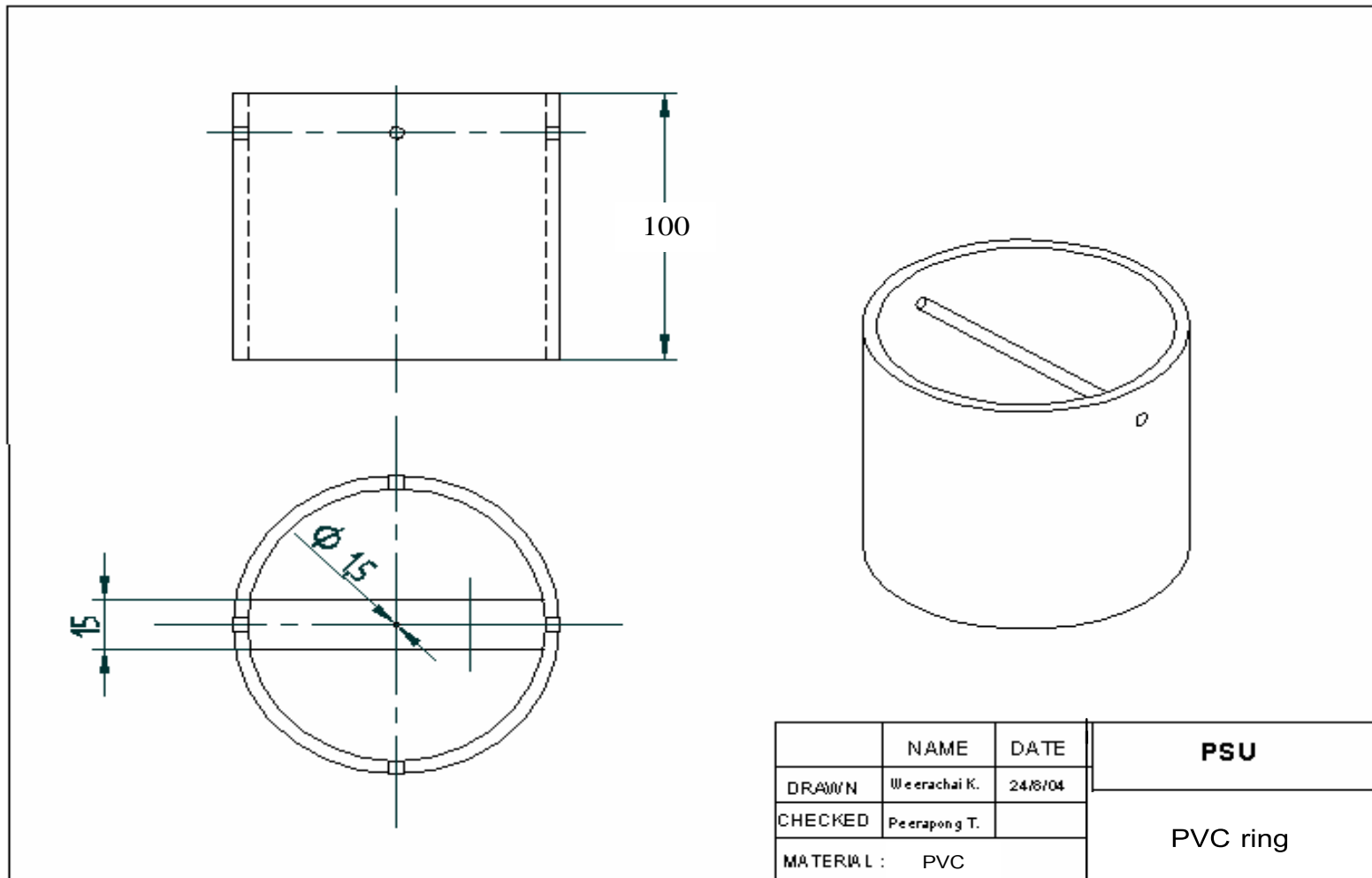


# **Appendix A**

## Drawing of ESP



**Figure 1.** Model of the designed ESP.



**Figure 2.** Model of PVC ring.

# **Appendix B**

Input-output data

**Table 6.** The measured data of input-output voltage

Measure no. 1			
VAC (Volt)	DC-peak (Volt)		Average (kVDC)
	Min.	Max.	
0	0	0	0
20	300	1300	800
40	500	2000	1250
60	700	1800	1250
80	800	4000	2400
100	1100	5500	3300
120	1400	6400	3900
140	1600	7500	4550
160	1800	8100	4950
180	2400	9000	5700
200	3200	10200	6700
220	3300	12500	7900

Measure no. 2			
VAC (Volt)	DC-peak (Volt)		Average (kVDC)
	Min.	Max.	
0	0	0	0
20	300	1300	800
40	500	2100	1300
60	700	2700	1700
80	800	3900	2350
100	1000	5200	3100
120	1300	6000	3650
140	1400	7300	4350
160	1700	8000	4850
180	2400	9400	5900
200	3100	10300	6700
220	3200	11900	7550

## **Appendix C**

Discharge current at various supply voltages

**Table 7.** The measured data of discharge current at various supply voltages

Clean ESP			
VAC [V]	I [ $\mu$ A]		
	1	2	3
0	0	0	0
20	0	0	0
40	0	0	0
60	0	0	0
80	0	*	*
100	*	*	*
120	*	*	*
140	*	*	*
160	*	*	*
180	1.3	1.5	1.2
200	19	19	19
220	31	29	30

Dust-loaded ESP			
VAC [V]	I [ $\mu$ A]		
	1	2	3
0	0	0	0
20	0	0	0
40	0	0	0
60	0	0	0
80	0	0	0
100	0	0	0
120	0	0	0
140	0	0	0
160	0	0	0
180	0	0	0
200	13	15	15
220	25	25	24

Note \* can not be read accurately.

## **Appendix D**

Collection efficiency data



Q = 2.83 lpm (V=1.04 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	36418	22656	13762	37.79
2	34370	20648	13722	39.92
4	33021	20140	12881	39.01
6	30259	17670	12589	41.60
average	33517	20279	13239	39.58
SD	2582.25	2050.41	593.71	1.61

Q = 10.83 lpm (V=3.77 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	39069	34966	4103	10.50
3	38120	35218	2902	7.61
5	37957	34544	3413	8.99
6	38957	35973	2984	7.66
average	38526	35175	3351	8.69
SD	568.39	600.14	549.44	1.37

Q = 20.06 lpm (V=7.36 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	41042	37280	3762	9.17
2	40977	38682	2295	5.60
4	40650	38383	2267	5.58
5	40707	37101	3606	8.86
average	40844	37862	2983	7.30
SD	194.33	787.76	812.60	1.98

Q = 30.03 lpm (V=11.02 cm/s)				
no.	upstream	downstream	different	% Efficiency
3	35227	33909	1318	3.74
4	35638	32244	3394	9.52
5	35495	34346	1149	3.24
6	35708	32334	3374	9.45
average	35517	33208	2309	6.49
SD	212.69	1076.97	1243.53	3.47

Q = 40.01 lpm (V=14.68 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	30028	28966	1062	3.54
3	29572	27451	2121	7.17
4	29677	28401	1276	4.30
5	29944	28230	1714	5.72
average	29805	28262	1543	5.18
SD	215.81	625.48	471.16	1.61

V ; cm/s	% Efficiency	SD
1.04	39.58	1.61
3.77	8.69	1.37
7.36	7.30	1.98
11.02	6.49	3.47
14.68	5.18	1.61

Q = 2.83 lpm (V=1.04 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	34866	16898	17968	51.53
3	33795	16208	17587	52.04
4	34193	16142	18051	52.79
5	33692	15988	17704	52.55
average	34137	16309	17828	52.23
SD	532.15	403.34	218.16	0.56

Q = 10.83 lpm (V=3.77 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	43010	35151	7859	18.27
3	42594	34691	7903	18.55
5	43022	35099	7923	18.42
6	43240	35151	8089	18.71
average	42967	35023	7944	18.49
SD	269.90	222.69	100.62	0.19

Q = 20.06 lpm (V=7.36 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	38860	35754	3106	7.99
4	39525	36690	2835	7.17
5	39708	36838	2870	7.23
6	39721	35715	4006	10.09
average	39454	36249	3204	8.12
SD	405.66	597.66	547.88	1.36

Q = 30.03 lpm (V=11.02 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	35429	33599	1830	5.17
3	35102	32926	2176	6.20
4	35900	33815	2085	5.81
5	35678	33653	2025	5.68
average	35527	33498	2029	5.71
SD	342.62	392.39	146.47	0.43

Q = 40.01 lpm (V=14.68 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	29100	28163	937	3.22
2	29271	28445	826	2.82
4	29064	27821	1243	4.28
6	28966	27886	1080	3.73
average	29100	28079	1022	3.51
SD	127.14	285.67	180.60	0.63

V ; cm/s	% Efficiency	SD
1.04	52.23	0.56
3.77	18.49	0.19
7.36	8.12	1.36
11.02	5.71	0.43
14.68	3.51	0.63

Q = 2.83 lpm (V=1.04 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	34900	8430	26470	75.85
3	34664	8883	25781	74.37
4	36227	8448	27779	76.68
6	36088	7260	28828	79.88
average	35470	8255	27215	76.70
SD	801.98	695.77	1357.85	2.33

Q = 10.83 lpm (V=3.77 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	40222	21069	19153	47.62
2	39647	20266	19381	48.88
3	41142	21480	19662	47.79
5	40604	20036	20568	50.66
average	40404	20713	19691	48.74
SD	630.03	676.55	620.62	1.40

Q = 20.06 lpm (V=7.36 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	42880	23725	19155	44.67
3	42946	24863	18083	42.11
4	42823	23673	19150	44.72
5	42478	23227	19251	45.32
average	42782	23872	18910	44.20
SD	208.64	697.45	553.12	1.43

Q = 30.03 lpm (V=11.02 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	34802	24005	10797	31.02
3	36526	23209	13317	36.46
4	32421	23053	9368	28.89
6	36550	23578	12972	35.49
average	35075	23461	11614	32.97
SD	1949.30	424.10	1866.94	3.60

Q = 40.01 lpm (V=14.68 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	29144	20521	8623	29.59
3	29738	20574	9164	30.82
4	29876	20839	9037	30.25
5	29592	20669	8923	30.15
average	29588	20651	8937	30.20
SD	317.59	139.64	231.17	0.50

V ; cm/s	% Efficiency	SD
1.04	76.70	2.33
3.77	48.74	1.40
7.36	44.20	1.43
11.02	32.97	3.60
14.68	30.20	0.50

Q = 2.83 lpm (V=1.04 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	35029	46	34983	99.87
2	34447	37	34410	99.89
3	33405	59	33346	99.82
6	32476	43	32433	99.87
average	33839	46	33793	99.86
SD	1130.18	9.29	1132.28	0.03

Q = 10.28 lpm (V=3.77 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	40482	352	40130	99.13
3	40145	441	39704	98.90
4	40267	360	39907	99.11
5	40827	322	40505	99.21
average	40430	369	40062	99.09
SD	298.95	50.87	343.06	0.13

Q = 20.06 lpm (V=7.36 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	42633	3069	39564	92.80
3	42306	2765	39541	93.46
4	42670	2586	40084	93.94
5	42451	3269	39182	92.30
average	42515	2922	39593	93.13
SD	169.04	305.27	371.28	0.72

Q = 30.03 lpm (V=11.02 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	36439	9517	26922	73.88
2	36492	9602	26890	73.69
4	36317	10373	25944	71.44
5	35803	8516	27287	76.21
average	36263	9502	26761	73.81
SD	315.14	761.81	573.51	1.95

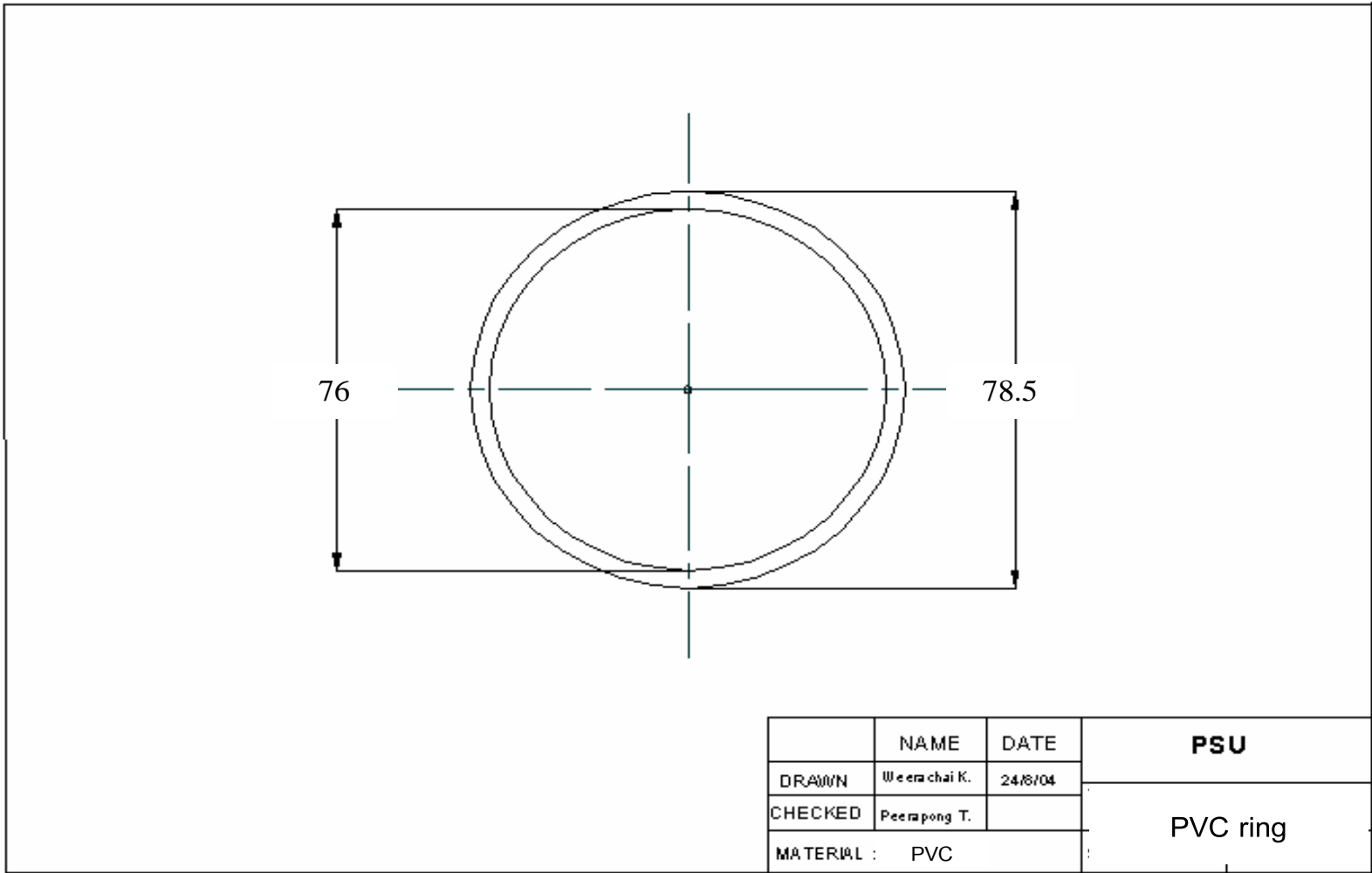
Q = 40.01 lpm (V=14.68 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	29810	11207	18603	62.41
2	29363	11414	17949	61.13
4	29149	9683	19466	66.78
5	28886	9838	19048	65.94
average	29302	10536	18767	64.06
SD	390.83	901.10	648.99	2.73

V ; cm/s	% Efficiency	SD
1.04	99.86	0.03
3.77	99.09	0.13
7.36	93.13	0.72
11.02	73.81	1.95
14.68	64.06	2.73









**Figure 3.** Model of PVC ring (continued).





Q = 2.83 lpm (V=1.04 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	42334	30939	11395	26.92
2	42023	31571	10452	24.87
3	43850	32869	10981	25.04
5	42575	31872	10703	25.14
average	42696	31813	10883	25.49
SD	802.15	804.37	404.11	0.96

Q = 10.83 lpm (V=3.77 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	35836	30577	5259	14.68
3	35943	30777	5166	14.37
4	35761	30921	4840	13.53
5	35638	30287	5351	15.01
average	35795	30641	5154	14.40
SD	128.31	274.66	222.54	0.63

Q = 20.06 lpm (V=7.36 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	37359	33769	3590	9.61
2	37357	33866	3491	9.34
4	37292	34926	2366	6.34
6	37052	35042	2010	5.42
average	37265	34401	2864	7.68
SD	145.37	676.30	795.30	2.11

Q = 30.03 lpm (V=11.02 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	30940	29310	1630	5.27
3	31512	29989	1523	4.83
5	31220	29385	1835	5.88
6	31346	29623	1723	5.50
average	31255	29577	1678	5.37
SD	241.37	305.51	132.92	0.44

Q = 40.01 lpm (V=14.68 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	32272	31675	597	1.85
3	32029	31481	548	1.71
4	32325	31746	579	1.79
6	32482	30768	1714	5.28
average	32277	31418	860	2.66
SD	187.85	447.25	570.03	1.75

V ; cm/s	% Efficiency	SD
1.04	25.49	0.96
3.77	14.40	0.63
7.36	7.68	2.11
11.02	5.37	0.44
14.68	2.66	1.75

Q = 2.83 lpm (V=1.04 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	40154	22344	17810	44.35
3	41654	23125	18529	44.48
5	42671	23553	19118	44.80
6	41442	23615	17827	43.02
average	41480	23159	18321	44.17
SD	1034.16	585.53	628.13	0.79

Q = 10.83 lpm (V=3.77 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	36086	30793	5293	14.67
3	36345	29484	6861	18.88
4	35962	29538	6424	17.86
6	36051	29403	6648	18.44
average	36111	29805	6307	17.46
SD	164.50	661.33	698.83	1.91

Q = 20.06 lpm (V=7.36 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	36998	34225	2773	7.49
3	37026	34422	2604	7.03
4	37353	34334	3019	8.08
5	37147	34224	2923	7.87
average	37131	34301	2830	7.62
SD	161.51	95.63	181.38	0.46

Q = 30.03 lpm (V=11.02 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	31612	29714	1898	6.00
3	31584	29859	1725	5.46
5	31738	30159	1579	4.98
6	31245	29698	1547	4.95
average	31545	29858	1687	5.35
SD	210.76	213.65	160.45	0.50

Q = 40.01 lpm (V=14.68 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	33096	31043	2053	6.20
4	33454	31642	1812	5.42
5	33348	31454	1894	5.68
6	33506	31495	2011	6.00
average	33351	31409	1943	5.83
SD	182.27	256.69	109.98	0.35

V ; cm/s	% Efficiency	SD
1.04	44.17	0.79
3.77	17.46	1.91
7.36	7.62	0.46
11.02	5.35	0.50
14.68	5.83	0.35

Q = 2.83 lpm (V=1.04 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	38843	12365	26478	68.17
2	38965	12509	26456	67.90
4	38102	13745	24357	63.93
5	38902	12262	26640	68.48
average	38703	12720	25983	67.13
SD	403.75	690.64	1086.93	2.14

Q = 10.83 lpm (V=3.77 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	36729	17958	18771	51.11
3	36553	16341	20212	55.30
4	35882	20378	15504	43.21
5	36190	17851	18339	50.67
average	36339	18132	18207	50.07
SD	378.13	1669.47	1971.61	5.03

Q = 20.06 lpm (V=7.36 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	37128	23741	13387	36.06
2	36762	23554	13208	35.93
4	36884	23886	12998	35.24
5	36963	24363	12600	34.09
average	36934	23886	13048	35.33
SD	153.36	345.82	338.49	0.90

Q = 30.03 lpm (V=11.02 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	31532	22873	8659	27.46
3	31859	22377	9482	29.76
4	31693	21844	9849	31.08
5	31671	21832	9839	31.07
average	31689	22232	9457	29.84
SD	134.03	497.48	558.87	1.70

Q = 40.01 lpm (V=14.68 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	33302	24653	8649	25.97
3	33588	25027	8561	25.49
4	33354	24127	9227	27.66
5	33007	24388	8619	26.11
average	33313	24549	8764	26.31
SD	238.79	384.41	310.82	0.94

V ; cm/s	% Efficiency	SD
1.04	67.13	2.14
3.77	50.07	5.03
7.36	35.33	0.90
11.02	29.84	1.70
14.68	26.31	0.94

Q = 2.83 lpm (V=1.04 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	43854	25	43829	99.94
4	41882	30	41852	99.93
5	43559	24	43535	99.94
6	43302	25	43277	99.94
เฉลี่ย	43149	26	43123	99.94
SD	874.42	2.71	876.99	0.01

Q = 10.83 lpm (V=3.77 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	36410	432	35978	98.81
3	36056	478	35578	98.67
4	36211	243	35968	99.33
5	36401	324	36077	99.11
เฉลี่ย	36270	369	35900	98.98
SD	169.35	106.07	220.39	0.29

Q = 20.06 lpm (V=7.36 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	36957	10417	26540	71.81
3	36956	9573	27383	74.10
5	36995	9963	27032	73.07
6	37380	9318	28062	75.07
เฉลี่ย	37072	9818	27254	73.51
SD	206.13	479.53	639.94	1.40

Q = 30.03 lpm (V=11.02 cm/s)				
no.	upstream	downstream	different	% Efficiency
1	31670	12789	18881	59.62
3	31765	13085	18680	58.81
4	32102	11680	20422	63.62
6	31369	12315	19054	60.74
เฉลี่ย	31727	12467	19259	60.70
SD	301.93	613.21	790.09	2.10

Q = 40.01 lpm (V=14.68 cm/s)				
no.	upstream	downstream	different	% Efficiency
2	33225	17506	15719	47.31
4	33402	16238	17164	51.39
5	33200	17215	15985	48.15
6	33436	16420	17016	50.89
เฉลี่ย	33316	16845	16471	49.43
SD	120.46	611.80	725.48	2.01

V ; cm/s	% Efficiency	SD
1.04	99.94	0.01
3.77	98.98	0.29
7.36	73.51	1.40
11.02	60.70	2.10
14.68	49.43	2.01

**Table 12.** Collection efficiency data for 0.5 micrometer at 100 VAC

Q = 2.83 lpm (V=1.04 cm/s)												
diameter ; $\mu\text{m}$	upstream						downstream					
	1	2	3	4	5	6	1	2	3	4	5	6
0.3	16080	15928	15715	16029	16102	15941	12319	11199	11860	12690	10807	11677
0.5	42334	42023	43850	41372	42575	41599	30939	31571	32869	30877	31872	31990
0.7	3110	3140	3215	3113	3200	3312	2326	2105	2254	2188	2302	2249
1.0	1710	1820	1911	1672	1718	1848	1334	1166	1098	1042	1246	1170
5.0	0	0	0	0	0	0	0	0	0	0	0	0

Q = 10.28 lpm (V=3.77 cm/s)												
diameter ; $\mu\text{m}$	upstream						downstream					
	1	2	3	4	5	6	1	2	3	4	5	6
0.3	16772	16907	16805	18616	22160	22851	17587	17778	17442	18732	18329	18222
0.5	35836	36386	35943	35761	35638	35478	30577	32090	30777	30921	30287	35454
0.7	3609	3733	3706	3668	3672	3558	3668	3464	3510	3610	3639	3671
1.0	1651	1604	1629	1687	1747	1700	1657	1597	1591	1632	1627	1601
5.0	0	0	0	1	0	0	0	0	0	0	0	0

Q = 20.06 lpm (V=7.36 cm/s)												
diameter ; $\mu\text{m}$	upstream						downstream					
	1	2	3	4	5	6	1	2	3	4	5	6
0.3	19416	19021	19376	19361	19020	18821	21540	22503	22553	22699	22467	22615
0.5	37359	37357	37506	37292	36881	37052	33769	33866	35070	34926	36056	35042
0.7	3961	3947	3997	4048	3964	3936	3804	3799	3852	3739	3890	3823
1.0	1809	1848	1802	1798	1728	1693	1672	1759	1712	1762	1763	1703
5.0	0	0	0	0	0	0	0	0	0	0	3	0

Q = 30.03 lpm (V=11.02 cm/s)												
diameter ; $\mu\text{m}$	upstream						downstream					
	1	2	3	4	5	6	1	2	3	4	5	6
0.3	17265	16788	16852	16641	16695	16672	21386	21258	20869	21229	21163	20761
0.5	31333	30940	31512	31146	31220	31346	31139	29310	29989	30565	29385	29623
0.7	3317	3348	3397	3255	3388	3291	3141	3174	3264	3154	3203	3113
1.0	1509	1469	1537	1467	1500	1522	1380	1425	1412	1445	1419	1418
5.0	0	0	0	0	0	0	0	0	0	0	0	0

Q = 40.01 lpm (V=14.68 cm/s)												
diameter ; $\mu\text{m}$	upstream						downstream					
	1	2	3	4	5	6	1	2	3	4	5	6
0.3	17959	17907	17655	18014	17648	17980	23538	23339	22659	23236	23297	22904
0.5	32349	32272	32029	32325	32288	32482	31522	31675	31481	31746	32053	30768
0.7	3385	3497	3377	3414	3478	3401	3306	3269	3203	3338	3327	3340
1.0	1568	1593	1544	1526	1504	1513	1465	1542	1492	1439	1510	1513
5.0	0	1	0	0	0	0	1	0	0	2	0	0

## **Appendix E**

Theoretical calculations for collection efficiency

## Collection Efficiency of ESP for 0.3 $\mu\text{m}$ at 180 VAC

ClearAll["Global`\*"]

### Some constants

$i=1 \cdot 10^{-6}$ ; (\* corona discharge current \*)

$dp=0.3 \cdot 10^{-6}$ ; (\* particle diameter \*)

$\lambda=0.066 \cdot 10^{-6}$ ; (\* mean free path \*)

$r=3.8 \cdot 10^{-2}$ ; (\* radius of the cylinder \*)

$d=7.6 \cdot 10^{-2}$ ; (\* diameter of the cylinder \*)

$L=24.5 \cdot 10^{-2}$ ; (\* length of the cylinder \*)

$k=1.38 \cdot 10^{-23}$ ; (\* Boltzmann's constant \*)

Temp=293; (\* temperature \*)

$\mu=1.820 \cdot 10^{-5}$ ; (\* viscosity \*)

$e=1.6 \cdot 10^{-19}$ ; (\* electron charge \*)

$\epsilon=2.4$ ; (\* dielectric constant of PSL \*)

### Geometry

volume= $\text{Pi} \cdot r^2 \cdot L$ ; (\* volume of the cylinder \*)

$A1=2 \cdot \text{Pi} \cdot r \cdot L$ ; (\* surface area of the cylinder \*)

$A2=(\text{Pi} \cdot d^2)/4$ ; (\* cross section area of the cylinder \*)

### Electric field strength inside a cylindrical tube:EE (180 V)

W=8833.33; (\* Voltage \*)

$R=3.8 \cdot 10^{-2}$ ;

$dw=0.5 \cdot 10^{-3}$ ;

$dt=7.6 \cdot 10^{-2}$ ;

$EE=W/(R \cdot \text{Log}[dt/dw])$ ;

### Cunningham correction factor

$Cc=1+2.52 \lambda/dp$ ;



**Time, Velocity, Flow**

$$Q[qq\_]=qq*10^{-3}/60;$$

$$V=Q[qq]/A2;$$

$$t=volume/Q[qq];$$

**Diffusion charging**

$$Ni=i/(e*Zi*EE*A1); (* ion concentration *)$$

$$\epsilon_0=8.8542*10^{-12}; (* vacuum permittivity *)$$

$$kE=(4 \text{ Pi } \epsilon_0)^{-1}; (* electrostatic constant *)$$

$$ci=9.79*10^3 \mu^{0.5} \text{Temp}^{0.5}; (* ion mean thermal velocity *)$$

$$ndiff[qq\_]=dp*k*Temp/(2*kE*e^2)*\text{Log}[1+(Pi*kE*dp*ci*e^2*Ni*t)/(2*k*Temp)];$$

**Field charging**

$$Zi=1.7*10^{-4}; (* mobility of ions *)$$

$$nfield[qq\_]=(3*\epsilon_0)/(\epsilon_0+2) * (EE*dp^2)/(4*kE*e) *$$

$$(Pi*kE*e*Zi*Ni*t/(1+Pi*kE*e*Zi*Ni*t));$$

**Combined Charging**

$$nall[qq\_]=ndiff[qq]+nfield[qq];$$

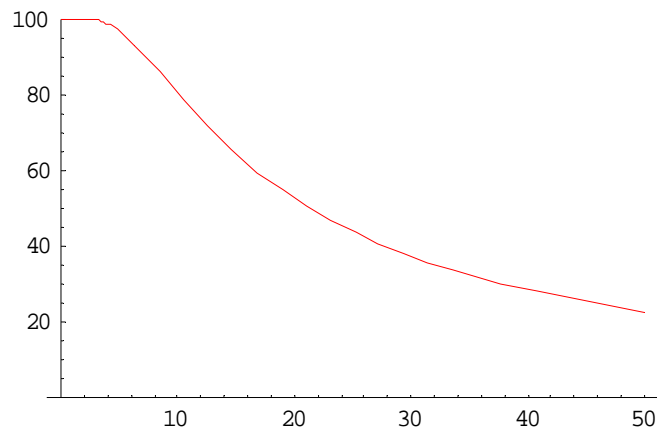
**Terminal electric velocity**

$$VTE[qq\_]=nall[qq]*e*EE*Cc/(3*Pi*\mu*dp);$$

**Collection efficiency**

$$\text{Eff}[qq\_]=(1-\text{Exp}[-VTE[qq]*A1/Q[qq]])*100;$$

$$\text{plot3}=\text{Plot}[\text{Eff}[qq],\{qq,0,50\},\text{PlotRange}\rightarrow\{0,100\},\text{PlotStyle}\rightarrow\text{RGBColor}[1,0,0]]$$



**Table 21.** Theoretical calculation data for 0.3  $\mu\text{m}$  at 180 VAC

V [cm/s]	Efficiency [%]
1.04	99.87
3.77	79.51
7.36	52.46
11.02	37.41
14.68	28.58

## Collection Efficiency of ESP for 0.5 $\mu\text{m}$ at 220 VAC

ClearAll["Global`\*"]

### Some constants

$i=35 \cdot 10^{-6}$ ; (\* corona discharge current \*)

$dp=0.5 \cdot 10^{-6}$ ; (\* particle diameter \*)

$\lambda=0.066 \cdot 10^{-6}$ ; (\* mean free path \*)

$r=3.8 \cdot 10^{-2}$ ; (\* radius of the cylinder \*)

$d=7.6 \cdot 10^{-2}$ ; (\* diameter of the cylinder \*)

$L=24.5 \cdot 10^{-2}$ ; (\* length of the cylinder \*)

$k=1.38 \cdot 10^{-23}$ ; (\* Boltzmann's constant \*)

Temp=293; (\* temperature \*)

$\mu=1.820 \cdot 10^{-5}$ ; (\* viscosity \*)

$e=1.6 \cdot 10^{-19}$ ; (\* electron charge \*)

$\epsilon=2.4$ ; (\* dielectric constant of PSL \*)

### Geometry

volume= $\text{Pi} \cdot r^2 \cdot L$ ; (\* volume of the cylinder \*)

$A1=2 \cdot \text{Pi} \cdot r \cdot L$ ; (\* surface area of the cylinder \*)

$A2=(\text{Pi} \cdot d^2)/4$ ; (\* cross section area of the cylinder \*)

### Electric field strength inside a cylindrical tube:EE (220 V)

W=11733.33; (\* Voltage \*)

$R=3.8 \cdot 10^{-2}$ ;

$dw=0.5 \cdot 10^{-3}$ ;

$dt=7.6 \cdot 10^{-2}$ ;

$EE=W/(R \cdot \text{Log}[dt/dw])$ ;

### Cunningham correction factor

$Cc=1+2.52 \lambda/dp$ ;

**Time, Velocity, Flow**

$$Q[\text{qq}_]=\text{qq} \cdot 10^{-3}/60;$$

$$V=Q[\text{qq}]/A2;$$

$$t=\text{volume}/Q[\text{qq}];$$

**Diffusion charging**

$$N_i=i/(e \cdot Z_i \cdot EE \cdot A1); \text{ (* ion concentration *)}$$

$$\epsilon_0=8.8542 \cdot 10^{-12}; \text{ (* vacuum permittivity *)}$$

$$kE=(4 \cdot \text{Pi} \cdot \epsilon_0)^{-1}; \text{ (* electrostatic constant *)}$$

$$c_i=9.79 \cdot 10^3 \cdot \mu^{0.5} \cdot \text{Temp}^{0.5}; \text{ (* ion mean thermal velocity *)}$$

$$\text{ndiff}[\text{qq}_]=\text{dp} \cdot k \cdot \text{Temp}/(2 \cdot kE \cdot e^2) \cdot \text{Log}[1+(\text{Pi} \cdot kE \cdot \text{dp} \cdot c_i \cdot e^2 \cdot N_i \cdot t)/(2 \cdot k \cdot \text{Temp})];$$

**Field charging**

$$Z_i=1.7 \cdot 10^{-4}; \text{ (* mobility of ions *)}$$

$$\text{nfield}[\text{qq}_]=(3 \cdot \epsilon_0)/(\epsilon_0+2) \cdot (EE \cdot \text{dp}^2)/(4 \cdot kE \cdot e) \cdot$$

$$(\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t)/(1+\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t);$$

**Combined Charging**

$$\text{nall}[\text{qq}_]=\text{ndiff}[\text{qq}]+\text{nfield}[\text{qq}];$$

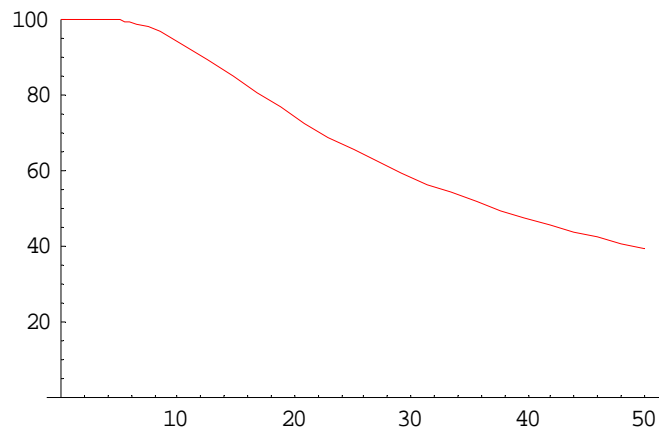
**Terminal electric velocity**

$$\text{VTE}[\text{qq}_]=\text{nall}[\text{qq}] \cdot e \cdot EE \cdot Cc/(3 \cdot \text{Pi} \cdot \mu \cdot \text{dp});$$

**Collection efficiency**

$$\text{Eff}[\text{qq}_]=(1-\text{Exp}[-\text{VTE}[\text{qq}] \cdot A1/Q[\text{qq}]]) \cdot 100;$$

$$\text{plot3}=\text{Plot}[\text{Eff}[\text{qq}],\{\text{qq},0,50\},\text{PlotRange} \rightarrow \{0,100\},\text{PlotStyle} \rightarrow \text{RGBColor}[1,0,0]]$$



**Table 22.** Theoretical calculation data for 0.5  $\mu\text{m}$  at 220 VAC

V [cm/s]	Efficiency [%]
1.04	100.00
3.77	93.91
7.36	74.25
11.02	58.30
14.68	47.26

## Collection Efficiency of ESP for 0.5 $\mu\text{m}$ at 180 VAC

ClearAll["Global`\*"]

### Some constants

$i=1 \cdot 10^{-6}$ ; (\* corona discharge current \*)  
 $dp=0.5 \cdot 10^{-6}$ ; (\* particle diameter \*)  
 $\lambda=0.066 \cdot 10^{-6}$ ; (\* mean free path \*)  
 $r=3.8 \cdot 10^{-2}$ ; (\* radius of the cylinder \*)  
 $d=7.6 \cdot 10^{-2}$ ; (\* diameter of the cylinder \*)  
 $L=24.5 \cdot 10^{-2}$ ; (\* length of the cylinder \*)  
 $k=1.38 \cdot 10^{-23}$ ; (\* Boltzmann's constant \*)  
 $\text{Temp}=293$ ; (\* temperature \*)  
 $\mu=1.820 \cdot 10^{-5}$ ; (\* viscosity \*)  
 $e=1.6 \cdot 10^{-19}$ ; (\* electron charge \*)  
 $\epsilon=2.4$ ; (\* dielectric constant of PSL \*)

### Geometry

$\text{volume}=\pi \cdot r^2 \cdot L$ ; (\* volume of the cylinder \*)  
 $A1=2 \cdot \pi \cdot r \cdot L$ ; (\* surface area of the cylinder \*)  
 $A2=(\pi \cdot d^2)/4$ ; (\* cross section area of the cylinder \*)

### Electric field strength inside a cylindrical tube:EE 180 V)

$W=8833.33$ ; (\* Voltage \*)  
 $R=3.8 \cdot 10^{-2}$ ;  
 $dw=0.5 \cdot 10^{-3}$ ;  
 $dt=7.6 \cdot 10^{-2}$ ;  
 $EE=W/(R \cdot \text{Log}[dt/dw])$ ;

### Cunningham correction factor

$Cc=1+2.52 \lambda/dp$ ;

**Time, Velocity, Flow**

$$Q[\text{qq}_]=\text{qq} \cdot 10^{-3}/60;$$

$$V=Q[\text{qq}]/A2;$$

$$t=\text{volume}/Q[\text{qq}];$$

**Diffusion charging**

$$N_i=i/(e \cdot Z_i \cdot EE \cdot A1); \text{ (* ion concentration *)}$$

$$\epsilon_0=8.8542 \cdot 10^{-12}; \text{ (* vacuum permittivity *)}$$

$$kE=(4 \cdot \text{Pi} \cdot \epsilon_0)^{-1}; \text{ (* electrostatic constant *)}$$

$$c_i=9.79 \cdot 10^3 \cdot \mu^{0.5} \cdot \text{Temp}^{0.5}; \text{ (* ion mean thermal velocity *)}$$

$$\text{ndiff}[\text{qq}_]=\text{dp} \cdot k \cdot \text{Temp}/(2 \cdot kE \cdot e^2) \cdot \text{Log}[1+(\text{Pi} \cdot kE \cdot \text{dp} \cdot c_i \cdot e^2 \cdot N_i \cdot t)/(2 \cdot k \cdot \text{Temp})];$$

**Field charging**

$$Z_i=1.7 \cdot 10^{-4}; \text{ (* mobility of ions *)}$$

$$\text{nfield}[\text{qq}_]=(3 \cdot \epsilon_0)/(\epsilon_0+2) \cdot (EE \cdot \text{dp}^2)/(4 \cdot kE \cdot e) \cdot$$

$$(\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t)/(1+\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t);$$

**Combined Charging**

$$\text{nall}[\text{qq}_]=\text{ndiff}[\text{qq}]+\text{nfield}[\text{qq}];$$

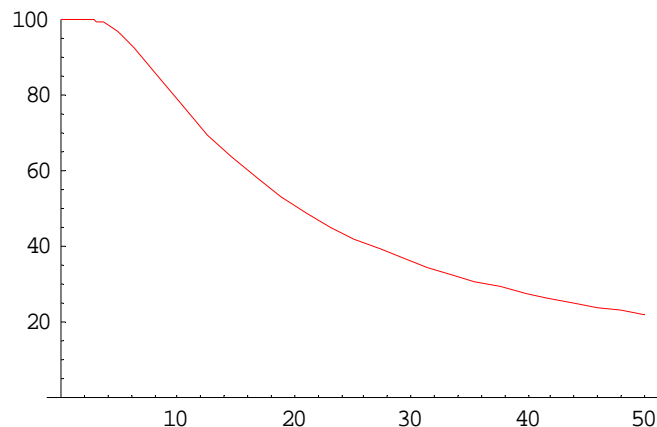
**Terminal electric velocity**

$$\text{VTE}[\text{qq}_]=\text{nall}[\text{qq}] \cdot e \cdot EE \cdot Cc/(3 \cdot \text{Pi} \cdot \mu \cdot \text{dp});$$

**Collection efficiency**

$$\text{Eff}[\text{qq}_]=(1-\text{Exp}[-\text{VTE}[\text{qq}] \cdot A1/Q[\text{qq}]]) \cdot 100;$$

$$\text{plot3}=\text{Plot}[\text{Eff}[\text{qq}],\{\text{qq},0,50\},\text{PlotRange} \rightarrow \{0,100\},\text{PlotStyle} \rightarrow \text{RGBColor}[1,0,0]]$$



**Table 23.** Theoretical calculation data for 0.5  $\mu\text{m}$  at 180 VAC

V [cm/s]	Efficiency [%]
1.04	99.80
3.77	77.64
7.36	50.76
11.02	36.16
14.68	27.66



## Collection Efficiency of ESP for 1.0 $\mu\text{m}$ at 220 VAC

ClearAll["Global`\*"]

### Some constants

$i=35 \cdot 10^{-6}$ ; (\* corona discharge current \*)

$dp=1.0 \cdot 10^{-6}$ ; (\* particle diameter \*)

$\lambda=0.066 \cdot 10^{-6}$ ; (\* mean free path \*)

$r=3.8 \cdot 10^{-2}$ ; (\* radius of the cylinder \*)

$d=7.6 \cdot 10^{-2}$ ; (\* diameter of the cylinder \*)

$L=24.5 \cdot 10^{-2}$ ; (\* length of the cylinder \*)

$k=1.38 \cdot 10^{-23}$ ; (\* Boltzmann's constant \*)

Temp=293; (\* temperature \*)

$\mu=1.820 \cdot 10^{-5}$ ; (\* viscosity \*)

$e=1.6 \cdot 10^{-19}$ ; (\* electron charge \*)

$\epsilon=2.4$ ; (\* dielectric constant of PSL \*)

### Geometry

volume= $\text{Pi} \cdot r^2 \cdot L$ ; (\* volume of the cylinder \*)

$A1=2 \cdot \text{Pi} \cdot r \cdot L$ ; (\* surface area of the cylinder \*)

$A2=(\text{Pi} \cdot d^2)/4$ ; (\* cross section area of the cylinder \*)

### Electric field strength inside a cylindrical tube:EE (220 V)

W=11733.33; (\* Voltage \*)

$R=3.8 \cdot 10^{-2}$ ;

$dw=0.5 \cdot 10^{-3}$ ;

$dt=7.6 \cdot 10^{-2}$ ;

$EE=W/(R \cdot \text{Log}[dt/dw])$ ;

### Cunningham correction factor

$Cc=1+2.52 \lambda/dp$ ;

**Time, Velocity, Flow**

$$Q[\text{qq}_]=\text{qq} \cdot 10^{-3}/60;$$

$$V=Q[\text{qq}]/A2;$$

$$t=\text{volume}/Q[\text{qq}];$$

**Diffusion charging**

$$N_i=i/(e \cdot Z_i \cdot EE \cdot A1); \text{ (* ion concentration *)}$$

$$\epsilon_0=8.8542 \cdot 10^{-12}; \text{ (* vacuum permittivity *)}$$

$$kE=(4 \cdot \text{Pi} \cdot \epsilon_0)^{-1}; \text{ (* electrostatic constant *)}$$

$$c_i=9.79 \cdot 10^3 \cdot \mu^{0.5} \cdot \text{Temp}^{0.5}; \text{ (* ion mean thermal velocity *)}$$

$$\text{ndiff}[\text{qq}_]=\text{dp} \cdot k \cdot \text{Temp}/(2 \cdot kE \cdot e^2) \cdot \text{Log}[1+(\text{Pi} \cdot kE \cdot \text{dp} \cdot c_i \cdot e^2 \cdot N_i \cdot t)/(2 \cdot k \cdot \text{Temp})];$$

**Field charging**

$$Z_i=1.7 \cdot 10^{-4}; \text{ (* mobility of ions *)}$$

$$\text{nfield}[\text{qq}_]=(3 \cdot \epsilon_0)/(\epsilon_0+2) \cdot (EE \cdot \text{dp}^2)/(4 \cdot kE \cdot e) \cdot$$

$$(\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t)/(1+\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t);$$

**Combined Charging**

$$\text{nall}[\text{qq}_]=\text{ndiff}[\text{qq}]+\text{nfield}[\text{qq}];$$

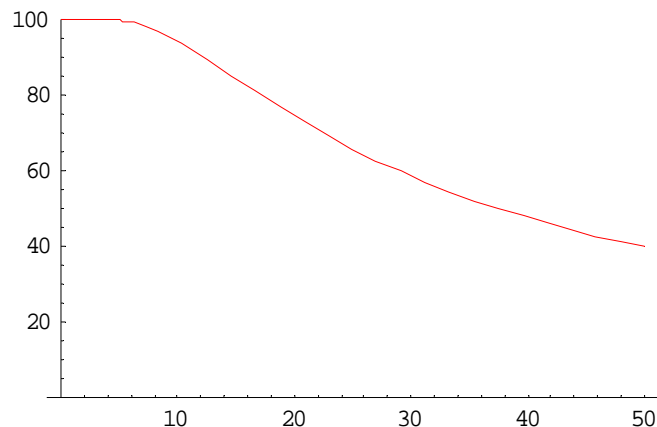
**Terminal electric velocity**

$$\text{VTE}[\text{qq}_]=\text{nall}[\text{qq}] \cdot e \cdot EE \cdot Cc/(3 \cdot \text{Pi} \cdot \mu \cdot \text{dp});$$

**Collection efficiency**

$$\text{Eff}[\text{qq}_]=(1-\text{Exp}[-\text{VTE}[\text{qq}] \cdot A1/Q[\text{qq}]]) \cdot 100;$$

$$\text{plot3}=\text{Plot}[\text{Eff}[\text{qq}],\{\text{qq},0,50\},\text{PlotRange} \rightarrow \{0,100\},\text{PlotStyle} \rightarrow \text{RGBColor}[1,0,0]]$$



**Table 24.** Theoretical calculation data for 1.0  $\mu\text{m}$  at 220 VAC

V [cm/s]	Efficiency [%]
1.04	100.00
3.77	93.84
7.36	74.36
11.02	58.58
14.68	47.63

## Collection Efficiency of ESP for 1.0 $\mu\text{m}$ at 180 VAC

ClearAll["Global`\*"]

### Some constants

$i=1 \cdot 10^{-6}$ ; (\* corona discharge current \*)

$dp=1.0 \cdot 10^{-6}$ ; (\* particle diameter \*)

$\lambda=0.066 \cdot 10^{-6}$ ; (\* mean free path \*)

$r=3.8 \cdot 10^{-2}$ ; (\* radius of the cylinder \*)

$d=7.6 \cdot 10^{-2}$ ; (\* diameter of the cylinder \*)

$L=24.5 \cdot 10^{-2}$ ; (\* length of the cylinder \*)

$k=1.38 \cdot 10^{-23}$ ; (\* Boltzmann's constant \*)

Temp=293; (\* temperature \*)

$\mu=1.820 \cdot 10^{-5}$ ; (\* viscosity \*)

$e=1.6 \cdot 10^{-19}$ ; (\* electron charge \*)

$\epsilon=2.4$ ; (\* dielectric constant of PSL \*)

### Geometry

volume= $\text{Pi} \cdot r^2 \cdot L$ ; (\* volume of the cylinder \*)

$A1=2 \cdot \text{Pi} \cdot r \cdot L$ ; (\* surface area of the cylinder \*)

$A2=(\text{Pi} \cdot d^2)/4$ ; (\* cross section area of the cylinder \*)

### Electric field strength inside a cylindrical tube:EE (180 V)

W=8833.33; (\* Voltage \*)

$R=3.8 \cdot 10^{-2}$ ;

$dw=0.5 \cdot 10^{-3}$ ;

$dt=7.6 \cdot 10^{-2}$ ;

$EE=W/(R \cdot \text{Log}[dt/dw])$ ;

### Cunningham correction factor

$Cc=1+2.52 \lambda/dp$ ;

**Time, Velocity, Flow**

$$Q[\text{qq}_]=\text{qq} \cdot 10^{-3}/60;$$

$$V=Q[\text{qq}]/A2;$$

$$t=\text{volume}/Q[\text{qq}];$$

**Diffusion charging**

$$N_i=i/(e \cdot Z_i \cdot EE \cdot A1); \text{ (* ion concentration *)}$$

$$\epsilon_0=8.8542 \cdot 10^{-12}; \text{ (* vacuum permittivity *)}$$

$$kE=(4 \cdot \text{Pi} \cdot \epsilon_0)^{-1}; \text{ (* electrostatic constant *)}$$

$$c_i=9.79 \cdot 10^3 \cdot \mu^{0.5} \cdot \text{Temp}^{0.5}; \text{ (* ion mean thermal velocity *)}$$

$$\text{ndiff}[\text{qq}_]=\text{dp} \cdot k \cdot \text{Temp}/(2 \cdot kE \cdot e^2) \cdot \text{Log}[1+(\text{Pi} \cdot kE \cdot \text{dp} \cdot c_i \cdot e^2 \cdot N_i \cdot t)/(2 \cdot k \cdot \text{Temp})];$$

**Field charging**

$$Z_i=1.7 \cdot 10^{-4}; \text{ (* mobility of ions *)}$$

$$\text{nfield}[\text{qq}_]=(3 \cdot \epsilon_0)/(\epsilon_0+2) \cdot (EE \cdot \text{dp}^2)/(4 \cdot kE \cdot e) \cdot$$

$$(\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t)/(1+\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t);$$

**Combined Charging**

$$\text{nall}[\text{qq}_]=\text{ndiff}[\text{qq}]+\text{nfield}[\text{qq}];$$

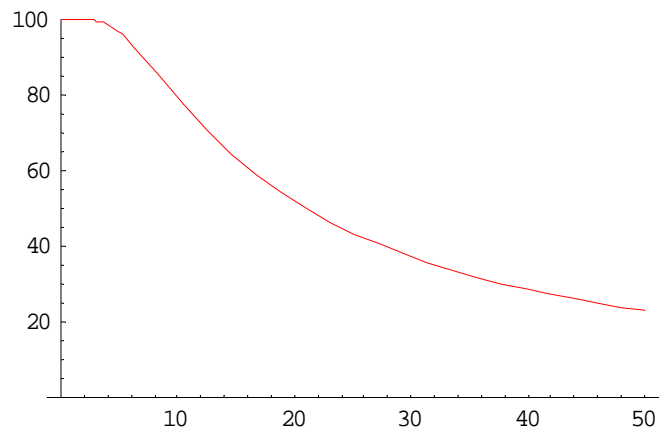
**Terminal electric velocity**

$$VTE[\text{qq}_]=\text{nall}[\text{qq}] \cdot e \cdot EE \cdot Cc/(3 \cdot \text{Pi} \cdot \mu \cdot \text{dp});$$

**Collection efficiency**

$$\text{Eff}[\text{qq}_]=(1-\text{Exp}[-VTE[\text{qq}] \cdot A1/Q[\text{qq}]]) \cdot 100;$$

$$\text{plot3}=\text{Plot}[\text{Eff}[\text{qq}],\{\text{qq},0,50\},\text{PlotRange} \rightarrow \{0,100\},\text{PlotStyle} \rightarrow \text{RGBColor}[1,0,0]]$$



**Table 25.** Theoretical calculation data for 1.0  $\mu\text{m}$  at 220 VAC

V [cm/s]	Efficiency [%]
1.04	99.80
3.77	78.28
7.36	51.81
11.02	37.24
14.68	28.67

## Collection Efficiency of ESP for 0.3 $\mu\text{m}$ at 180 VAC

ClearAll["Global`\*"]

### Some constants

$i=1 \cdot 10^{-6}$ ; (\* corona discharge current \*)  
 $dp=0.3 \cdot 10^{-6}$ ; (\* particle diameter \*)  
 $\lambda=0.066 \cdot 10^{-6}$ ; (\* mean free path \*)  
 $r=3.8 \cdot 10^{-2}$ ; (\* radius of the cylinder \*)  
 $d=7.6 \cdot 10^{-2}$ ; (\* diameter of the cylinder \*)  
 $L=24.5 \cdot 10^{-2}$ ; (\* length of the cylinder \*)  
 $k=1.38 \cdot 10^{-23}$ ; (\* Boltzmann's constant \*)  
 $\text{Temp}=293$ ; (\* temperature \*)  
 $\mu=1.820 \cdot 10^{-5}$ ; (\* viscosity \*)  
 $e=1.6 \cdot 10^{-19}$ ; (\* electron charge \*)  
 $\epsilon=2.4$ ; (\* dielectric constant of PSL \*)

### Geometry

$\text{volume}=\pi \cdot r^2 \cdot L$ ; (\* volume of the cylinder \*)  
 $A1=2 \cdot \pi \cdot r \cdot L$ ; (\* surface area of the cylinder \*)  
 $A2=(\pi \cdot d^2)/4$ ; (\* cross section area of the cylinder \*)

### Electric field strength inside a cylindrical tube:EE (180 V)

$W=8833.33$ ; (\* Voltage \*)  
 $R=3.8 \cdot 10^{-2}$ ;  
 $dw=0.5 \cdot 10^{-3}$ ;  
 $dt=7.6 \cdot 10^{-2}$ ;  
 $EE=W/(R \cdot \text{Log}[dt/dw])$ ;

### Cunningham correction factor

$Cc=1+2.52 \lambda/dp$ ;

**Time, Velocity, Flow**

$$Q[qq\_]=qq*10^{-3}/60;$$

$$V=Q[qq]/A2;$$

$$t=volume/Q[qq];$$

**Diffusion charging**

$$Ni=i/(e*Zi*EE*A1); (* ion concentration *)$$

$$\epsilon_0=8.8542*10^{-12}; (* vacuum permittivity *)$$

$$kE=(4 \text{ Pi } \epsilon_0)^{-1}; (* electrostatic constant *)$$

$$ci=9.79*10^3 \mu^{0.5} \text{Temp}^{0.5}; (* ion mean thermal velocity *)$$

$$ndiff[qq\_]=dp*k*Temp/(2*kE*e^2)*\text{Log}[1+(Pi*kE*dp*ci*e^2*Ni*t)/(2*k*Temp)];$$

**Field charging**

$$Zi=1.7*10^{-4}; (* mobility of ions *)$$

$$nfield[qq\_]=(3*\epsilon_0)/(\epsilon_0+2) * (EE*dp^2)/(4*kE*e) *$$

$$(Pi*kE*e*Zi*Ni*t/(1+Pi*kE*e*Zi*Ni*t));$$

**Combined Charging**

$$nall[qq\_]=ndiff[qq]+nfield[qq];$$

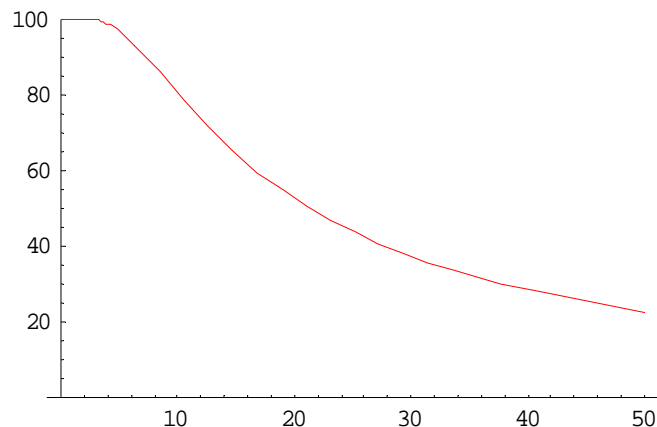
**Terminal electric velocity**

$$VTE[qq\_]=nall[qq]*e*EE*Cc/(3*Pi*\mu*dp);$$

**Collection efficiency**

$$\text{Eff}[qq\_]=(1-\text{Exp}[-VTE[qq]*A1/Q[qq]])*100;$$

$$\text{plot3}=\text{Plot}[\text{Eff}[qq],\{qq,0,50\},\text{PlotRange}\rightarrow\{0,100\},\text{PlotStyle}\rightarrow\text{RGBColor}[1,0,0]]$$





**Table 21.** Theoretical calculation data for 0.3  $\mu\text{m}$  at 180 VAC

V [cm/s]	Efficiency [%]
1.04	99.87
3.77	79.51
7.36	52.46
11.02	37.41
14.68	28.58

## Collection Efficiency of ESP for 0.5 $\mu\text{m}$ at 220 VAC

ClearAll["Global`\*"]

### Some constants

$i=35 \cdot 10^{-6}$ ; (\* corona discharge current \*)

$dp=0.5 \cdot 10^{-6}$ ; (\* particle diameter \*)

$\lambda=0.066 \cdot 10^{-6}$ ; (\* mean free path \*)

$r=3.8 \cdot 10^{-2}$ ; (\* radius of the cylinder \*)

$d=7.6 \cdot 10^{-2}$ ; (\* diameter of the cylinder \*)

$L=24.5 \cdot 10^{-2}$ ; (\* length of the cylinder \*)

$k=1.38 \cdot 10^{-23}$ ; (\* Boltzmann's constant \*)

Temp=293; (\* temperature \*)

$\mu=1.820 \cdot 10^{-5}$ ; (\* viscosity \*)

$e=1.6 \cdot 10^{-19}$ ; (\* electron charge \*)

$\epsilon=2.4$ ; (\* dielectric constant of PSL \*)

### Geometry

volume= $\text{Pi} \cdot r^2 \cdot L$ ; (\* volume of the cylinder \*)

$A1=2 \cdot \text{Pi} \cdot r \cdot L$ ; (\* surface area of the cylinder \*)

$A2=(\text{Pi} \cdot d^2)/4$ ; (\* cross section area of the cylinder \*)

### Electric field strength inside a cylindrical tube:EE (220 V)

W=11733.33; (\* Voltage \*)

$R=3.8 \cdot 10^{-2}$ ;

$dw=0.5 \cdot 10^{-3}$ ;

$dt=7.6 \cdot 10^{-2}$ ;

$EE=W/(R \cdot \text{Log}[dt/dw])$ ;

### Cunningham correction factor

$Cc=1+2.52 \lambda/dp$ ;

**Time, Velocity, Flow**

$$Q[\text{qq}_]=\text{qq} \cdot 10^{-3}/60;$$

$$V=Q[\text{qq}]/A2;$$

$$t=\text{volume}/Q[\text{qq}];$$

**Diffusion charging**

$$N_i=i/(e \cdot Z_i \cdot EE \cdot A1); \text{ (* ion concentration *)}$$

$$\epsilon_0=8.8542 \cdot 10^{-12}; \text{ (* vacuum permittivity *)}$$

$$kE=(4 \cdot \text{Pi} \cdot \epsilon_0)^{-1}; \text{ (* electrostatic constant *)}$$

$$c_i=9.79 \cdot 10^3 \cdot \mu^{0.5} \cdot \text{Temp}^{0.5}; \text{ (* ion mean thermal velocity *)}$$

$$\text{ndiff}[\text{qq}_]=\text{dp} \cdot k \cdot \text{Temp}/(2 \cdot kE \cdot e^2) \cdot \text{Log}[1+(\text{Pi} \cdot kE \cdot \text{dp} \cdot c_i \cdot e^2 \cdot N_i \cdot t)/(2 \cdot k \cdot \text{Temp})];$$

**Field charging**

$$Z_i=1.7 \cdot 10^{-4}; \text{ (* mobility of ions *)}$$

$$\text{nfield}[\text{qq}_]=(3 \cdot \epsilon_0)/(\epsilon_0+2) \cdot (EE \cdot \text{dp}^2)/(4 \cdot kE \cdot e) \cdot$$

$$(\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t)/(1+\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t);$$

**Combined Charging**

$$\text{nall}[\text{qq}_]=\text{ndiff}[\text{qq}]+\text{nfield}[\text{qq}];$$

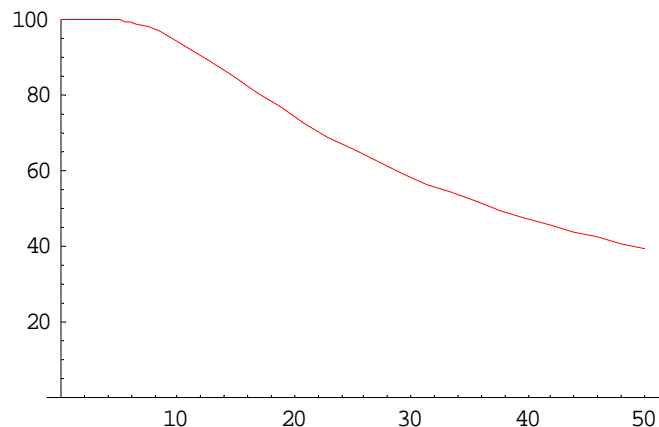
**Terminal electric velocity**

$$\text{VTE}[\text{qq}_]=\text{nall}[\text{qq}] \cdot e \cdot EE \cdot Cc/(3 \cdot \text{Pi} \cdot \mu \cdot \text{dp});$$

**Collection efficiency**

$$\text{Eff}[\text{qq}_]=(1-\text{Exp}[-\text{VTE}[\text{qq}] \cdot A1/Q[\text{qq}]]) \cdot 100;$$

$$\text{plot3}=\text{Plot}[\text{Eff}[\text{qq}],\{\text{qq},0,50\},\text{PlotRange} \rightarrow \{0,100\},\text{PlotStyle} \rightarrow \text{RGBColor}[1,0,0]]$$



**Table 22.** Theoretical calculation data for 0.5  $\mu\text{m}$  at 220 VAC

V [cm/s]	Efficiency [%]
1.04	100.00
3.77	93.91
7.36	74.25
11.02	58.30
14.68	47.26

## Collection Efficiency of ESP for 0.5 $\mu\text{m}$ at 180 VAC

ClearAll["Global`\*"]

### Some constants

$i=1 \cdot 10^{-6}$ ; (\* corona discharge current \*)  
 $dp=0.5 \cdot 10^{-6}$ ; (\* particle diameter \*)  
 $\lambda=0.066 \cdot 10^{-6}$ ; (\* mean free path \*)  
 $r=3.8 \cdot 10^{-2}$ ; (\* radius of the cylinder \*)  
 $d=7.6 \cdot 10^{-2}$ ; (\* diameter of the cylinder \*)  
 $L=24.5 \cdot 10^{-2}$ ; (\* length of the cylinder \*)  
 $k=1.38 \cdot 10^{-23}$ ; (\* Boltzmann's constant \*)  
 $\text{Temp}=293$ ; (\* temperature \*)  
 $\mu=1.820 \cdot 10^{-5}$ ; (\* viscosity \*)  
 $e=1.6 \cdot 10^{-19}$ ; (\* electron charge \*)  
 $\epsilon=2.4$ ; (\* dielectric constant of PSL \*)

### Geometry

$\text{volume}=\pi \cdot r^2 \cdot L$ ; (\* volume of the cylinder \*)  
 $A1=2 \cdot \pi \cdot r \cdot L$ ; (\* surface area of the cylinder \*)  
 $A2=(\pi \cdot d^2)/4$ ; (\* cross section area of the cylinder \*)

### Electric field strength inside a cylindrical tube:EE 180 V)

$W=8833.33$ ; (\* Voltage \*)  
 $R=3.8 \cdot 10^{-2}$ ;  
 $dw=0.5 \cdot 10^{-3}$ ;  
 $dt=7.6 \cdot 10^{-2}$ ;  
 $EE=W/(R \cdot \text{Log}[dt/dw])$ ;

### Cunningham correction factor

$Cc=1+2.52 \lambda/dp$ ;

**Time, Velocity, Flow**

$$Q[\text{qq}_]=\text{qq} \cdot 10^{-3}/60;$$

$$V=Q[\text{qq}]/A2;$$

$$t=\text{volume}/Q[\text{qq}];$$

**Diffusion charging**

$$N_i=i/(e \cdot Z_i \cdot EE \cdot A1); \text{ (* ion concentration *)}$$

$$\epsilon_0=8.8542 \cdot 10^{-12}; \text{ (* vacuum permittivity *)}$$

$$kE=(4 \cdot \text{Pi} \cdot \epsilon_0)^{-1}; \text{ (* electrostatic constant *)}$$

$$c_i=9.79 \cdot 10^3 \cdot \mu^{0.5} \cdot \text{Temp}^{0.5}; \text{ (* ion mean thermal velocity *)}$$

$$\text{ndiff}[\text{qq}_]=\text{dp} \cdot k \cdot \text{Temp}/(2 \cdot kE \cdot e^2) \cdot \text{Log}[1+(\text{Pi} \cdot kE \cdot \text{dp} \cdot c_i \cdot e^2 \cdot N_i \cdot t)/(2 \cdot k \cdot \text{Temp})];$$

**Field charging**

$$Z_i=1.7 \cdot 10^{-4}; \text{ (* mobility of ions *)}$$

$$\text{nfield}[\text{qq}_]=(3 \cdot \epsilon_0)/(\epsilon_0+2) \cdot (EE \cdot \text{dp}^2)/(4 \cdot kE \cdot e) \cdot$$

$$(\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t)/(1+\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t);$$

**Combined Charging**

$$\text{nall}[\text{qq}_]=\text{ndiff}[\text{qq}]+\text{nfield}[\text{qq}];$$

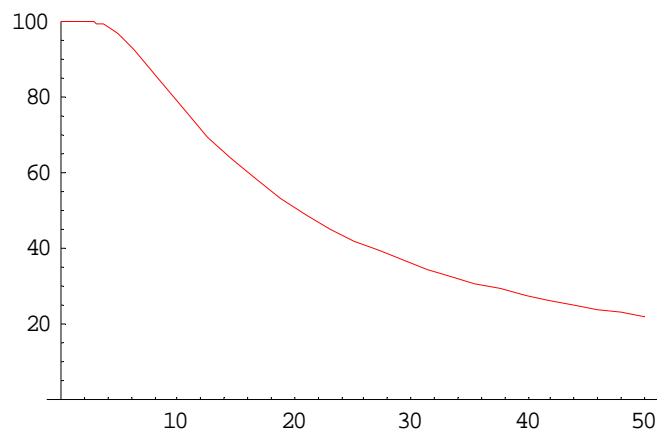
**Terminal electric velocity**

$$\text{VTE}[\text{qq}_]=\text{nall}[\text{qq}] \cdot e \cdot EE \cdot Cc/(3 \cdot \text{Pi} \cdot \mu \cdot \text{dp});$$

**Collection efficiency**

$$\text{Eff}[\text{qq}_]=(1-\text{Exp}[-\text{VTE}[\text{qq}] \cdot A1/Q[\text{qq}]]) \cdot 100;$$

$$\text{plot3}=\text{Plot}[\text{Eff}[\text{qq}],\{\text{qq},0,50\},\text{PlotRange} \rightarrow \{0,100\},\text{PlotStyle} \rightarrow \text{RGBColor}[1,0,0]]$$



**Table 23.** Theoretical calculation data for 0.5  $\mu\text{m}$  at 180 VAC

V [cm/s]	Efficiency [%]
1.04	99.80
3.77	77.64
7.36	50.76
11.02	36.16
14.68	27.66

## Collection Efficiency of ESP for 1.0 $\mu\text{m}$ at 220 VAC

ClearAll["Global`\*"]

### Some constants

$i=35 \cdot 10^{-6}$ ; (\* corona discharge current \*)

$dp=1.0 \cdot 10^{-6}$ ; (\* particle diameter \*)

$\lambda=0.066 \cdot 10^{-6}$ ; (\* mean free path \*)

$r=3.8 \cdot 10^{-2}$ ; (\* radius of the cylinder \*)

$d=7.6 \cdot 10^{-2}$ ; (\* diameter of the cylinder \*)

$L=24.5 \cdot 10^{-2}$ ; (\* length of the cylinder \*)

$k=1.38 \cdot 10^{-23}$ ; (\* Boltzmann's constant \*)

Temp=293; (\* temperature \*)

$\mu=1.820 \cdot 10^{-5}$ ; (\* viscosity \*)

$e=1.6 \cdot 10^{-19}$ ; (\* electron charge \*)

$\epsilon=2.4$ ; (\* dielectric constant of PSL \*)

### Geometry

volume= $\text{Pi} \cdot r^2 \cdot L$ ; (\* volume of the cylinder \*)

$A1=2 \cdot \text{Pi} \cdot r \cdot L$ ; (\* surface area of the cylinder \*)

$A2=(\text{Pi} \cdot d^2)/4$ ; (\* cross section area of the cylinder \*)

### Electric field strength inside a cylindrical tube:EE (220 V)

W=11733.33; (\* Voltage \*)

$R=3.8 \cdot 10^{-2}$ ;

$dw=0.5 \cdot 10^{-3}$ ;

$dt=7.6 \cdot 10^{-2}$ ;

$EE=W/(R \cdot \text{Log}[dt/dw])$ ;

### Cunningham correction factor

$Cc=1+2.52 \lambda/dp$ ;



**Time, Velocity, Flow**

$$Q[\text{qq}_]=\text{qq} \cdot 10^{-3}/60;$$

$$V=Q[\text{qq}]/A2;$$

$$t=\text{volume}/Q[\text{qq}];$$

**Diffusion charging**

$$N_i=i/(e \cdot Z_i \cdot EE \cdot A1); \text{ (* ion concentration *)}$$

$$\epsilon_0=8.8542 \cdot 10^{-12}; \text{ (* vacuum permittivity *)}$$

$$kE=(4 \cdot \text{Pi} \cdot \epsilon_0)^{-1}; \text{ (* electrostatic constant *)}$$

$$c_i=9.79 \cdot 10^3 \cdot \mu^{0.5} \cdot \text{Temp}^{0.5}; \text{ (* ion mean thermal velocity *)}$$

$$\text{ndiff}[\text{qq}_]=\text{dp} \cdot k \cdot \text{Temp} / (2 \cdot kE \cdot e^2) \cdot \text{Log}[1 + (\text{Pi} \cdot kE \cdot \text{dp} \cdot c_i \cdot e^2 \cdot N_i \cdot t) / (2 \cdot k \cdot \text{Temp})];$$

**Field charging**

$$Z_i=1.7 \cdot 10^{-4}; \text{ (* mobility of ions *)}$$

$$\text{nfield}[\text{qq}_]=(3 \cdot \epsilon_0) / (\epsilon_0 + 2) \cdot (EE \cdot \text{dp}^2) / (4 \cdot kE \cdot e) \cdot$$

$$(\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t / (1 + \text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t));$$

**Combined Charging**

$$\text{nall}[\text{qq}_]=\text{ndiff}[\text{qq}] + \text{nfield}[\text{qq}];$$

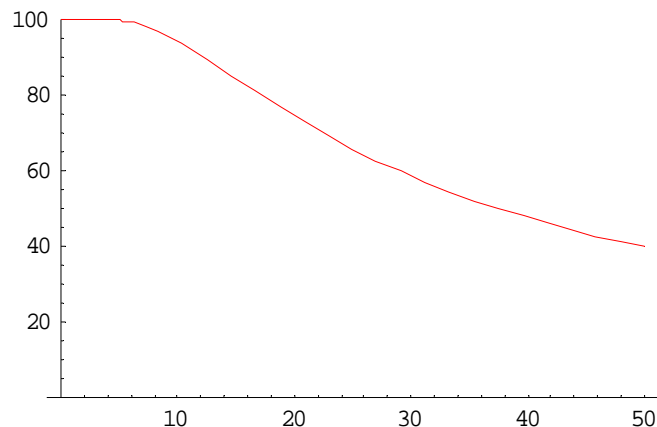
**Terminal electric velocity**

$$\text{VTE}[\text{qq}_]=\text{nall}[\text{qq}] \cdot e \cdot EE \cdot Cc / (3 \cdot \text{Pi} \cdot \mu \cdot \text{dp});$$

**Collection efficiency**

$$\text{Eff}[\text{qq}_]=(1 - \text{Exp}[-\text{VTE}[\text{qq}] \cdot A1 / Q[\text{qq}]]) \cdot 100;$$

$$\text{plot3}=\text{Plot}[\text{Eff}[\text{qq}], \{\text{qq}, 0, 50\}, \text{PlotRange} \rightarrow \{0, 100\}, \text{PlotStyle} \rightarrow \text{RGBColor}[1, 0, 0]]$$



**Table 24.** Theoretical calculation data for 1.0  $\mu\text{m}$  at 220 VAC

V [cm/s]	Efficiency [%]
1.04	100.00
3.77	93.84
7.36	74.36
11.02	58.58
14.68	47.63

## Collection Efficiency of ESP for 1.0 $\mu\text{m}$ at 180 VAC

ClearAll["Global`\*"]

### Some constants

$i=1 \cdot 10^{-6}$ ; (\* corona discharge current \*)  
 $dp=1.0 \cdot 10^{-6}$ ; (\* particle diameter \*)  
 $\lambda=0.066 \cdot 10^{-6}$ ; (\* mean free path \*)  
 $r=3.8 \cdot 10^{-2}$ ; (\* radius of the cylinder \*)  
 $d=7.6 \cdot 10^{-2}$ ; (\* diameter of the cylinder \*)  
 $L=24.5 \cdot 10^{-2}$ ; (\* length of the cylinder \*)  
 $k=1.38 \cdot 10^{-23}$ ; (\* Boltzmann's constant \*)  
 $\text{Temp}=293$ ; (\* temperature \*)  
 $\mu=1.820 \cdot 10^{-5}$ ; (\* viscosity \*)  
 $e=1.6 \cdot 10^{-19}$ ; (\* electron charge \*)  
 $\epsilon=2.4$ ; (\* dielectric constant of PSL \*)

### Geometry

$\text{volume}=\pi \cdot r^2 \cdot L$ ; (\* volume of the cylinder \*)  
 $A1=2 \cdot \pi \cdot r \cdot L$ ; (\* surface area of the cylinder \*)  
 $A2=(\pi \cdot d^2)/4$ ; (\* cross section area of the cylinder \*)

### Electric field strength inside a cylindrical tube:EE (180 V)

$W=8833.33$ ; (\* Voltage \*)  
 $R=3.8 \cdot 10^{-2}$ ;  
 $dw=0.5 \cdot 10^{-3}$ ;  
 $dt=7.6 \cdot 10^{-2}$ ;  
 $EE=W/(R \cdot \text{Log}[dt/dw])$ ;

### Cunningham correction factor

$Cc=1+2.52 \lambda/dp$ ;

**Time, Velocity, Flow**

$$Q[\text{qq}_-]=\text{qq} \cdot 10^{-3}/60;$$

$$V=Q[\text{qq}]/A2;$$

$$t=\text{volume}/Q[\text{qq}];$$

**Diffusion charging**

$$N_i=i/(e \cdot Z_i \cdot EE \cdot A1); \text{ (* ion concentration *)}$$

$$\epsilon_0=8.8542 \cdot 10^{-12}; \text{ (* vacuum permittivity *)}$$

$$kE=(4 \cdot \text{Pi} \cdot \epsilon_0)^{-1}; \text{ (* electrostatic constant *)}$$

$$c_i=9.79 \cdot 10^3 \cdot \mu^{0.5} \cdot \text{Temp}^{0.5}; \text{ (* ion mean thermal velocity *)}$$

$$\text{ndiff}[\text{qq}_-]=\text{dp} \cdot k \cdot \text{Temp}/(2 \cdot kE \cdot e^2) \cdot \text{Log}[1+(\text{Pi} \cdot kE \cdot \text{dp} \cdot c_i \cdot e^2 \cdot N_i \cdot t)/(2 \cdot k \cdot \text{Temp})];$$

**Field charging**

$$Z_i=1.7 \cdot 10^{-4}; \text{ (* mobility of ions *)}$$

$$\text{nfield}[\text{qq}_-]=(3 \cdot \epsilon_0)/(\epsilon_0+2) \cdot (EE \cdot \text{dp}^2)/(4 \cdot kE \cdot e) \cdot$$

$$(\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t)/(1+\text{Pi} \cdot kE \cdot e \cdot Z_i \cdot N_i \cdot t);$$

**Combined Charging**

$$\text{nall}[\text{qq}_-]=\text{ndiff}[\text{qq}] + \text{nfield}[\text{qq}];$$

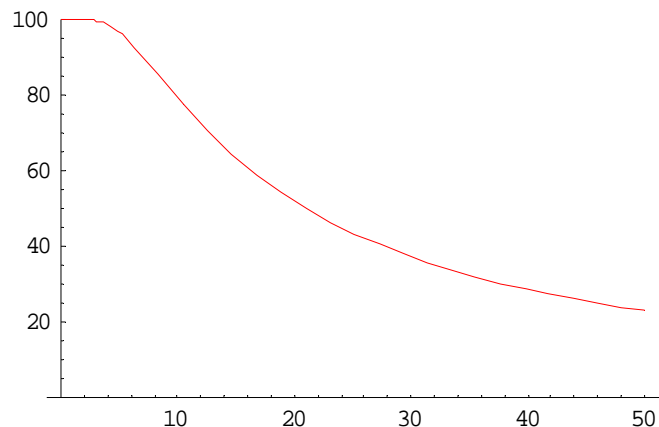
**Terminal electric velocity**

$$VTE[\text{qq}_-]=\text{nall}[\text{qq}] \cdot e \cdot EE \cdot Cc/(3 \cdot \text{Pi} \cdot \mu \cdot \text{dp});$$

**Collection efficiency**

$$\text{Eff}[\text{qq}_-]=(1-\text{Exp}[-VTE[\text{qq}] \cdot A1/Q[\text{qq}]]) \cdot 100;$$

$$\text{plot3}=\text{Plot}[\text{Eff}[\text{qq}],\{\text{qq},0,50\},\text{PlotRange} \rightarrow \{0,100\},\text{PlotStyle} \rightarrow \text{RGBColor}[1,0,0]]$$



**Table 25.** Theoretical calculation data for 1.0  $\mu\text{m}$  at 220 VAC

V [cm/s]	Efficiency [%]
1.04	99.80
3.77	78.28
7.36	51.81
11.02	37.24
14.68	28.67

# **Appendix F**

Pressure drop data

**Table 26.** Pressure drop data

Velocity, U (cm/s)	Pressure drop, $\Delta P$ (torr)			average	SD
	1	2	3		
1.04	0.02	0.03	0.03	0.03	0.01
3.77	0.02	0.03	0.03	0.03	0.01
7.36	0.02	0.03	0.03	0.03	0.01
11.02	0.03	0.03	0.04	0.03	0.01
14.68	0.03	0.03	0.04	0.03	0.01

**Appendix G**  
Dust-loading data



**Table 27.** Dust-loading data

<b>t (s)</b>	<b>M<sub>ESP,initial</sub> (g)</b>	<b>M<sub>ESP,final</sub> (g)</b>	<b>ΔM<sub>ESP</sub> (g)</b>	<b>Accumulative dust-loading</b>
30	1574.00	1579.07	5.07	5.07
60	1579.07	1583.67	4.60	9.67
90	1583.67	1587.94	4.27	13.94
120	1587.94	1592.00	4.06	18.00
150	1592.00	1595.14	3.14	21.14
180	1595.14	1598.34	3.20	24.34
210	1598.34	1601.64	3.30	27.64
240	1601.64	1605.28	3.64	31.28
270	1605.28	1608.74	3.46	34.74
300	1608.74	1611.38	2.64	37.38
330	1611.38	1614.18	2.8	40.18
360	1614.18	1616.54	2.36	42.54
390	1616.54	1619.31	2.77	45.31
420	1619.31	1621.93	2.62	47.93
450	1621.93	1624.06	2.13	50.06
480	1624.06	1625.11	1.05	51.11
510	1625.11	1626.57	1.46	52.57
540	1626.57	1627.63	1.06	53.63
570	1627.63	1628.54	0.91	54.54
600	1628.54	1628.92	0.38	54.92

Note  $M_{ESP,initial}$  is initial mass of the ESP and  $M_{ESP,final}$  is final mass of the ESP, respectively.

Table 28. Cvt data

t [s]	M <sub>initial</sub> [g]	M <sub>final</sub> [g]	C [kg/m <sup>3</sup> ]	v [m/s]	E [%]	Cvt [kg/m <sup>2</sup> ]
1800	0.2567	0.0650	0.0004	0.0735	74.6786	0.0566
3600	0.0783	0.0261	0.0001	0.0735	66.6667	0.0345
5400	0.1283	0.0454	0.0002	0.0735	64.6142	0.0849
7200	0.1615	0.0665	0.0003	0.0735	58.8235	0.1425
9000	0.2049	0.0881	0.0003	0.0735	57.0034	0.2260
10800	0.3204	0.1432	0.0005	0.0735	55.3059	0.4240
12600	0.1259	0.0674	0.0002	0.0735	46.4654	0.1944
14400	0.1736	0.0945	0.0003	0.0735	45.5645	0.3063
16200	0.2351	0.1330	0.0004	0.0735	43.4283	0.4667
18000	0.2250	0.1309	0.0004	0.0735	41.8222	0.4962
19800	0.2162	0.1272	0.0004	0.0735	41.1656	0.5245
21600	0.1181	0.0714	0.0002	0.0735	39.5428	0.3126
23400	0.2958	0.1826	0.0005	0.0735	38.2691	0.8481
25200	0.2373	0.1472	0.0004	0.0735	37.9688	0.7327
27000	0.0891	0.0554	0.0001	0.0735	37.8227	0.2948
28800	0.1496	0.0977	0.0002	0.0735	34.6925	0.5279
30600	0.1966	0.1584	0.0003	0.0735	19.4303	0.7371
32400	0.1035	0.0838	0.0002	0.0735	19.0338	0.4109
34200	0.0744	0.0610	0.0001	0.0735	18.0108	0.3118
36000	0.1174	0.0971	0.0002	0.0735	17.2913	0.5178

## **Appendix H**

Laboratory collection efficiency for dust-loaded ESP

Table 29. Collection efficiency data for 1.0 micrometer with dust-loading for 30 minutes at 220 VAC

diameter : $\mu\text{m}$	Q = 2.83 lpm (V=1.04 cm/s)											
	upstream						downstream					
	1	2	3	4	5	6	1	2	3	4	5	6
0.3	13266	15051	14650	15313	15405	15328	152	71	15	18	20	23
0.5	16048	17294	17806	19654	19401	19401	104	104	19	19	15	17
0.7	20606	21681	21775	24138	25170	25769	227	108	15	12	15	16
1.0	54244	59519	60454	70016	69083	68560	502	230	238	219	211	224
5.0	2	6	3	1	2	2	0	0	0	0	0	0

diameter : $\mu\text{m}$	Q = 10.28 lpm (V=3.77 cm/s)											
	upstream						downstream					
	1	2	3	4	5	6	1	2	3	4	5	6
0.3	9245	9049	8780	9628	9195	9317	327	340	277	277	237	254
0.5	12544	12943	11580	12417	13069	13203	300	261	211	152	157	158
0.7	16719	17609	14711	16580	18079	18345	330	341	295	139	204	199
1.0	43609	45704	39905	44146	45887	46169	1490	1769	1844	1784	1686	1477
5.0	2	0	1	2	0	2	0	0	0	0	0	0

diameter : $\mu\text{m}$	Q = 20.06 lpm (V=7.36 cm/s)											
	upstream						downstream					
	1	2	3	4	5	6	1	2	3	4	5	6
0.3	7469	7596	7508	7486	7778	7704	549	606	436	446	439	435
0.5	10396	10065	10161	10295	11061	10212	401	458	560	560	401	503
0.7	14483	14125	13530	14541	14962	14451	533	663	580	633	504	536
1.0	35403	36384	36201	36388	36928	36997	6933	7337	6803	7271	7203	7294
5.0	1	0	3	2	0	0	0	0	0	0	0	0

diameter : $\mu\text{m}$	Q = 30.03 lpm (V=11.02 cm/s)											
	upstream						downstream					
	1	2	3	4	5	6	1	2	3	4	5	6
0.3	6683	6268	6860	6420	6427	6665	1480	891	568	857	911	936
0.5	10065	8887	9170	8522	9644	9781	2103	1374	867	1294	1160	949
0.7	13698	12392	12995	11993	12980	13273	2289	1523	878	1383	1356	1257
1.0	31025	29373	31676	29666	30734	30898	14855	15514	12788	13241	13575	13704
5.0	0	0	0	4	5	2	0	0	0	0	0	0

diameter : $\mu\text{m}$	Q = 40.01 lpm (V=14.68 cm/s)											
	upstream						downstream					
	1	2	3	4	5	6	1	2	3	4	5	6
0.3	4909	5121	6673	6236	6402	5967	2828	2643	2593	2433	2939	2765
0.5	7440	7794	9329	8540	8768	8393	3314	3383	3895	3319	3376	2983
0.7	9888	10792	11860	11276	11309	10928	5197	4639	4597	4018	4717	4085
1.0	22336	223949	22052	24359	21853	24047	11629	12965	12808	14475	12792	12874
5.0	3	0	1	4	4	1	0	0	0	0	0	0

Q = 2.83 lpm				
no.	upstream	downstream	different	% Efficiency
2	59519	230	59289	99.61
3	60454	238	60216	99.61
4	70016	219	69797	99.69
6	68560	224	68336	99.67
average	64637	228	64410	99.65
SD	5416.49	8.18	5423.64	0.04

Q = 10.28 lpm				
no.	upstream	downstream	different	% Efficiency
2	45704	1769	43935	96.13
3	39905	1844	38061	95.38
4	44146	1784	42362	95.96
5	45887	1686	44201	96.33
average	43911	1771	42140	95.95
SD	2782.25	65.13	2837.68	0.41

Q = 20.06 lpm				
no.	upstream	downstream	different	% Efficiency
2	36384	7337	29047	79.83
4	36388	7271	29117	80.02
5	36928	7203	29725	80.49
6	36997	7294	29703	80.28
average	36674	7276	29398	80.16
SD	334.04	55.97	366.11	0.29

Q = 30.03 lpm				
no.	upstream	downstream	different	% Efficiency
3	31676	12788	18888	59.63
4	29666	13241	16425	55.37
5	30734	13575	17159	55.83
6	30898	13704	17194	55.65
average	30744	13327	17417	56.62
SD	827.55	408.88	1043.10	2.02

Q = 40.01 lpm				
no.	upstream	downstream	different	% Efficiency
2	23949	12965	10984	45.86
3	22052	12808	9244	41.92
5	21853	12792	9061	41.46
6	24047	12874	11173	46.46
average	22975	12860	10116	43.93
SD	1184.44	78.63	1117.15	2.60

V : cm/s	% Efficiency	SD
1.04	99.65	0.04
3.77	95.97	0.41
7.36	80.16	0.29
11.02	56.62	2.02
14.68	43.93	2.60