# **Chapter 2**

# Methodology

This section describes the methods used, including an overview of the management of data, statistical methods for data analysis, geometric correction, management of land-use code and land-use cover, digitization, complex regions, and statistical analysis.

### 2.1 GIS data structure

The Thailand Department of Land Development has recorded millions of records for land-use data from regular surveys and Remote Sensing (RS). The data are stored in several types, which need to be combined to obtain thematic maps. Such maps can be created directly from these files using commercial software such as MapInfo and ArcGIS. Alternatively, the files can be restructured into relational database tables and used with general purpose programs such as R. For MapInfo or ArcGIS use, the files for Phuket in 2009 are as shown in Figure 1.

Name	Туре	Size			
lu_phuket_52	MID File	146 KB			
lu_phuket_52	MIF File	5,402 KB			

Figure 1. Files to illustrate thematic map from Thailand Department of Land Development.

To illustrate these files we focus on a subset comprising just one small island south of the Phuket mainland ("Coral Island") that contains 12 land-use plots. Note that each record in this MID file corresponds to a plot. The MID file has 8 fields. AREA is the total area in the polygon in square meters. PERIMETER is the total distance around the border of the polygon. LU\_CODE refers to type of land-use. DES\_TH and DES\_EN are descriptions in Thai and English. RAI, ACRES and HECTARES specify these units, as shown in Figure 2. Note that the file does not contain a primary key and is thus not a relational database table, but it can be converted to such a table simply by inserting an index field.

AREA P 87607.007 1 235285.827 2 242126.513 2 39322.12 7 17945.538 6 66632.936 1 10080.674 4 15269.779 4 86619.535 1 3091006.074 1 32929.351 1	PERIMETER 1763.417 2348.238 2934.426 744.409 565.325 101.126 161.133 192.801 1630.524 13333.328 1016.317	LU_CODE A405 A405 U201/A405 A302 A302 A302 A302 A302 A302 F101 A405 A302	DES_EN มะพร้าว หมู่บ้าน/มะพร้าว ยางพารา ยางพารา ยางพารา ยางพารา ยางพารา ยางพารา ปาดิบสมบูรณ์ มะพร้าว	DES_TH Coconut Coconut Village/Coconut Para rubber Para rubber Para rubber Para rubber Para rubber Para rubber Para rubber Dense evergreen forest Coconut	RAI 55 147 151 25 11 42 6 10 54 1932 21	ACRES 21.648 58.14 59.831 9.717 4.434 16.465 2.491 3.773 21.404 763.801 8.137	HECTARES 8.761 23.529 24.213 3.932 1.795 6.663 1.008 1.527 8.662 309.101 3.293
657247.445 6	5928.178	A302	มะพราว ยางพารา	Para rubber	411	162.409	65.725

Figure 2. Example of data structure of original form from MID file

The corresponding MIF (MapInfo Data Format) file contains values of the coordinates X, Y and other information. Again the records are not indexed, and their physical order needs to be the same as the plots in the MID file. Figure 3 illustrates this file structure for the Coral Island data. It contains 780 records. The first 15 records contain the names of the fields in the MID file, and the remaining 765 records comprise 12 groups corresponding to the plots in the MID file. The first record in each group is of the form "Region n", when n is 1 unless the plot contains "subplots" in which case n is the number of subplots. Subplots are of two kinds: "holes" and "islands". For example, group 10 in the MIF file contains four such holes, labeled 10a, 10b, 10c and 10d, so n is increased to 5. For each plot corresponding to a hole the data are duplicated: the same (X, Y) coordinates appear in plots 6, 8, 4 and 7, respectively. Note also that these coordinates are listed in clockwise order around the boundary of the plot, except that the duplicated points inside a plot are listed in the

reverse order to ensure that the total area is correct, because the formula for the area of a polygon gives a result with the opposite sign when the order of the boundary points is reversed. "Island" subplots are clusters of plots not contained in any plot; Coral Island does not contain any subplots with this property. Each group in the MIF file also contains three trailing records, which specify how the vectors are graphed in the map and the position of the centroid of each plot.

216 432231.26 860876.04 1 Version 3 2 Charset "WindowsThai" 513 430491.2 861302.04 10a 3 Delimiter "," 217 Pen (1,2,0) 514 32 Brush (1,0,16777215) 218 515 4 CoordSvs Earth Projection 8, 104, "m" 431899.79 861156.7 219 Center 432211.89 860947.07 5 Columns 8 ÷ 1 AREA Decimal(20, 3) 220 Region 546 431899.79 861156.7 PERIMETER Decimal(20, 3) 221 32 10b547 13 222 431899.79 861156.7 LU CODE Char(15) 548 431391.84 860189.45 DES\_TH Char (100) 223 431948.86 861130.02 431391.84 860170.51 560 431422.83 860170.51 560 431422.83 860153.29 : 560 431391.84 860189.45 10 DES EN Char (100) 224 431959.19 861099.03 6 ÷. 11 RAI Decimal(10, 0) ÷ 253 431899.79 861156.7 12 ACRES Decimal(20, 3) Pen (1,2,0) Brush (1,0,16777215) 13 HECTARES Decimal(20, 3) 254 10c561 14 14 Data 255 562 431397.01 860974.19 256 Center 431805.09 861072.76 15 563 431415.95 860955.26 257 Region 16 Region 1 564 431474.49 860951.81 17 42 258 18 259 431753.43 860754.66 18 432111.7 860268.58 575 431397.01 860974.19 19 432089.44 860313.53 260 431793.9 860775.31 576 10d 18 261 431823.17 860788.23 276 431753.43 860754.66 431741.38 860740.02 20 432092.44 860329.37 577 7 ł ÷ 578 431744.83 860709.03 E 579 431751.71 860697.83 59 432111.7 860268.58 277 Pen (1,2,0) ÷ 3 Pen (1,2,0) Brush (1,0,16777215) 60 278 Brush (1,0,16777215) 594 431741.38 860740.02 61 Center 431834.37 860741.31 279 Pen (1,2,0) 595 Center 432375.37 860592.64 62 280 Region Brush (1,0,16777215) 596 63 Region 281 14 597 Center 430623.23 860665 64 56 282 431419.4 861000.02 283 431441.77 861036.18 598 Region 65 429545.07 860886.26 599 12 66 429552.7 860940.57 284 431474.49 861046.51 600 430890.43 861470.53 2 67 429545.91 860966.87 8 ÷. . . 601 430920.05 861633.46 1 1 1 295 431419.4 861000.02 602 431044.03 861568.02 120 429545.07 860886.26 11 296 Pen (1,2,0) **i** 611 430890.43 861470.53 121 Pen (1,2,0) 297 Brush (1,0,16777215) Brush (1,0,16777215) 122 298 Center 431487.41 861005.18 612 Pen (1,2,0) 123 Center 429787.76 861226.52 299 Region 1 Brush (1,0,16777215) 613 124 Region 1 300 36 614 Center 431101.53 861545.64 125 46 301 432401.09 860271.57 615 Region 126 430484.42 861471.76 302 432420.78 860339.22 616 161 430462.35 861487.88 127 303 432432.77 860414.56 9 617 430890.43 861470.53 128 430446.23 861495.52 3 618 430945.35 861471.83 336 432401.09 860271.57 619 431025.08 861469.03 171 430484.42 861471.76 12 Pen (1,2,0) 337 ÷ 1 Pen (1,2,0) 172 Brush (1,0,16777215) 338 Brush (1,0,16777215) 777 430890.43 861470.53 173 Center 432548.21 860318.37 339 174 Center 430351.78 861579.73 778 Pen (1,2,0) 340 Region 5 Brush (1,0,16777215) 175 Region 1 779 172 341 Center 430744.78 861166.12 176 13 780 342 430491.2 861302.04 177 431412.5 860299.65 430527.47 861291.45 343 10 178 431450.38 860365.09 430539.51 861257.01 344 179 431479.66 860384.02 4 3 8 ÷ 189 431412.5 860299.65 19( Pen (1,2,0) Brush (1,0,16777215) 191 Center 431489.99 860262.63 192 193 Region 194 22 195 432231.26 860876.04 196 432212.32 860871.74 5 432152.9 860875.18

Figure 3. Data structure of MIF file in Coral Island (south of Phuket)

As is clear from Figure 3, the MIF file is not a relational database table because it is not indexed and it also contains a mixture of data and design information. To create thematic maps using a general purpose program, it is necessary to restructure the MIF file to be a relational database table. This new data structure is shown in Figure 4.



Figure 4. Data in Figure 3 after restructuring & indexing as a relational database table Figure 5 shows a map created from the data in Figure 4 using Excel. This map may be created by starting with the set of (X, Y) coordinates for plot 10 with cells containing

NAs omitted, and then adding separate points for the other 15 sets (including the sets for 10a, 10b, 10c and 10d, again omitting the cells containing NAs).



Figure 5. Map created from data in Figure 4 using Excel

# 2.2 Coordinate shifts (geometric correction)

Image Geometry Correction is the process of digitally manipulating image data so that the image's projection precisely matches a specific projection surface or shape. Data from RS needs to be checked for geometric correction because of distortion created by incorrect positioning. The standards for measuring GIS data have changed in recent decades. These coordinate shifts are quite substantial and complicate the accurate measurement of land-use change. Assuming that coordinates available from Google Earth maps are correct and that these locations have not changed substantially over recent decades, it is desirable to convert all land-use coordinates to agree with the corresponding Google Earth coordinates. The method we use for this conversion is based on a bilinear transformation of the form

$$u = a_1 + b_1 x + c_1 y + d_1 x y \tag{1}$$

$$v = a_2 + b_2 x + c_2 y + d_2 x y \tag{2}$$

In these equators (x, y) are coordinates in the files that need to be corrected and (u, v) are their corresponding corrected values that agree with Google coordinates.

The parameters  $(a_1, b_1, c_1, d_1, a_2, b_2, c_2, d_2)$  in equations (1) and (2) are determined by using the data for the coordinate shifts (dx, dy) at the four locations mapped in Figure 6. These equations are expressed in matrix form as

$$\boldsymbol{g} = \boldsymbol{F} \boldsymbol{h} \tag{3}$$

In this formulation g is the column vector  $(u_1, v_1, u_2, v_2, u_3, v_3, u_4, v_4)$ , h is the column vector  $(a_1, b_1, c_1, d_1, a_2, b_2, c_2, d_2)$  and F is an  $8 \times 8$  matrix, as follows.

$\begin{bmatrix} u_1\\ v_1\\ u_2\\ v_2\\ u_3\\ v_3\\ u_4\\ v_4 \end{bmatrix}$	P	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$y_1 = 0$ $y_2 = 0$ $y_3 = 0$ $y_4 = x$ $0$	$   \begin{array}{c} x_1 y \\ 0 \\ x_2 y \\ 0 \\ x_3 y \\ 0 \\ x_4 y \\ 0 \end{array} $	0 1 0 1 0 1 0 1 0	$0$ $x_1$ $0$ $x_2$ $0$ $x_3$ $0$ $x_4$	0 y <sub>1</sub> 0 y <sub>2</sub> 0 y <sub>3</sub> 0 y <sub>4</sub>	$ \begin{array}{c} 0\\ x_1y\\ 0\\ x_2y\\ 0\\ x_3y\\ 0\\ x_4y \end{array} $	×	$\begin{bmatrix} a_1\\b_1\\c_2\\d_2\\a_3\\b_3\\c_4\\d_4 \end{bmatrix}$	-



Figure 6. Geometric correction (in kilometers) of UTM coordinates positions based on land-use records recorded by the Thailand Department of Land Development in 1985 to those in Google Earth in 2011

Table 1 shows (x,y) coordinates of the location of the rectangle (coloured red) in the right panels, with corresponding (u,v) coordinates.

Table 1.	Coordinate	shifts in	Phuket	Island	based	on	informa	ation	in	Figure	6
										<u> </u>	

Rectangle Corner	х, у	km	u, v
North east	439.0, 892.0	-0.45, 0.30	438.55, 892.30
North west	420.0,871.0	-0.18, 0.12	420.18, 870.89
South east	439.0, 871.0	-0.35, 0.44	438.65, 871.44
South west	420.0, 871.0	-0.14,0.25	419.86, 871.25

# 2.3 Digitization concept

Polygonal shapes are difficult to use for analysis of land-use change because both the plot shapes and their data change. The left panel of Figure 7 shows thematic maps of land-use on Coral Island for 2000 and 2009. The top left panel shows the coordinate shift needed to make the reported and corrected maps agree using the bilinear transformation described in the preceding section. The right panel shows a 100×100 meter square grid to convert the polygonal shape file to raster format. The six points in the plot with plotID 397 in 2009 are (431.75, 861.15), (431.85, 861.05), (431.85, 861.05), (431.75, 861.95) and (431.85, 861.95) respectively.



Figure 7. Thematic map of land-use in Coral Island, Phuket, in 2000 (upper panel) and 2009 (lower panel) with 100×100 meter grid used for digitization.

The right panel of Figure 8 details a subset of the grid points within a  $5 \times 5$  matrix, which illustrates the comparison between the polygonal and digitized data structures. These data structures for the polygon with plotID 397 in 2009 are shown in Table 2 below.



Figure 8. Grid points in raster format for Coral Island in 2009 with details for

plotID 397

 Table 2: Data structures for polygonal (left table) and digitalized (right table) data

	Polygo	n (vector	Point (raster)					
plotID	pointID	x	у	x	у	plotID		
397	1	431.90	861.16	431.75	861.15	397		
397	2	431.95	861.13	431.85	861.15	397		
397	3	431.96	861.10	431.75	861.05	397		
397	4	431.96	861.07	431.85	861.05	397		
397	5	431.94	861.05	431.75	860.95	397		
397	6	431.92	861.04	431.85	860.95	397		
•	•	•	•					
		•						
397	30	431.82	861.17					
397	31	431.86	861.17					
397	32	431.90	861.16					

structures for plotID 397 in 2009

# 2.4 Digitization method

This section explains how to convert a polygonal shape file to a digitized data structure using a computer program. The computation involves assigning grid points to polygons. This pseudo code is

for each polygon pi in the specified region

label all grid points inside pi as i

end

This algorithm can be implemented in any language that accommodates *for...end* loops, provided the language has a function that determines which elements of a specified set of points contained within a specified polygon. The R program language has a library *sp* that contains a function *point.in.polygon()* documented below.

point in.polygon {sp} R Documentation
do point(s) fall in a given polygon? Description verifies for one or more points whether they fall in a given polygon Usage point.in.polygon(point.x. pol.x. pol.y. mode.checked=FALSE)
Arguments
point.x       numerical array of x-coordinates of points         point.y       numerical array of y-coordinates of points         pol.x       numerical array of x-coordinates of polygon         pol.y       numerical array of y-coordinates of polygon         mode.checked default FALSE, used internally to save time when all the other argument are known to be of storage mode double
Value
integer array; values are: 0: point is strictly exterior to pol; 1: point is strictly interior to pol; 2: point lies on the relative interior of an edge of pol; 3: point is a vertex of pol.
References
Uses the C function InPoly(). InPoly is Copyright (c) 1998 by Joseph O'Rourke. It may be freely redistributed in its entirety provided that this copyright notice is not removed.
Examples
<pre># open polygon: point.in.polygon(1:10,1:10,c(3,5,5,3),c(3,3,5,5)) # closed polygon: point.in.polygon(1:10,rep(4,10),c(3,5,5,3,3),c(3,3,5,5,3))</pre>

[Package sp version 1.0-5 Index]

Figure 9. Documentation for function *point.in.polygon()* in *sp* library for R

#### The program commands in Figure 10 show how to remove holes in a complex region

and assign the values of the plotIDs to grid points.

# digitize land-use for Phuket from analog form for 2009 # function to compute area of a polygon 1x <- length(x) sum((x[2:1x]-x[1:1x-1])\*(y[2:1x]+y[1:1x-1]))/2 } #holesFound <- 1
holesFound <- 0</pre> if (digitized==0 & holesFound==0) { read.table("luPhuket52.txt",h=T,as.is=T) -> p52data str(p52data) read.table("luPhuket52.xy",h=T,as.is=T) -> p52xy p52xy <- subset(p52xy,is.finite(p52xy\$x)) p52xy <- subset(p52xy,p52xy\$pointID>0) p52xy <- subset(p52xy,p52xy\$plotID>0) p52xy <- subset(p52xy,!is.na(p52xy\$x) & p52xy\$y==1)) p52xy\$x <- ifelse(is.na(p52xy\$y),NA,p52xy\$x) 2=F) juote=F) p52xy\$x <- p52xy\$x/1000 p52xy\$y <- p52xy\$y/1000 # convert meters to km # find plots with holes and delete the holes if (holesFound==0) rxya <- NA+p52xy[1,] for (j in p52data\$plotID) {
 rxy] <- subset(p52xy, p52xy\$plotID==j)
 rxj]AA <- subset(rxy], is.na(rxy]\$x))
 if (dim(rxy]NA\$[L]>0) {
 ptID1 <- min(rxy]NA\$pointID
 rxy] <- subset(rxy], rxy]\$pointID<ptID1)
 p52data\$hole[p52data\$plotID==j] <- 1
 }
}</pre> Campouls rxya <- rbind(rxya,rxyj) 🦳 🥼 rxy0 <- rxya[-1,] wrlte.table(rxy0,"phuket520K.xy",row.names=F,quote=F) wrlte.table(p52data,"phuket520K.txt",row.names=F,quote=F) }\_\_\_ if (digitized==0 & holesFound==1) { # region 1 (north of Phuket ) ymax <- 908; ymin <- 881; xmin <- 418; xmax <- 443 ncols <- (xmax-xmin)\*10 # specify grid nrows <- (ymax-ymin)\*10 pt.x <- xmin-0.05+0.1\*c(1:ncols)
pt.x <- rep(pt.x,nrows)</pre> pt.y <- ymax-0.05+0\*c(l:ncols) for (i in c(l:(nrows-1))) { pt.y <- c(pt.y,ymax-0.05-i\*0.1+0\*c(l:ncols)) } plotIDs <- 0\*pt.x # populate grid with plotIDs read.table("phuket520K.xy",h=T,as.is=T) -> Rxy
read.table("phuket520K.txt",h=T,as.is=T) -> Rdata rxy <- subset(Rxy,(Rxy\$x>xmin & Rxy\$x<xmax & Rxy\$y>ymin & Rxy\$y<ymax)) set <- unique(rxy\$plotID) rxy <- subset(Rxy,Rxy\$plotID %in% set) rd <- subset(Rdata,Rdata\$plotID %in% set) rd <- rd[order(rd\$area,decreasing=F),] plotIDs1 <- rd\$plotID library(sp) for (j in plotIDs1) {
 pol <- subset(rxy,rxy\$plotID==j)
 pol.x <- pol\$x
 poly <- pol\$y
 pol.y <- pol\$y
 pol.y <- pol\$y
 point.in.polygon(pt.x,pt.y,pol.x,pol.y) -> grid
 pointDs <- ifelse((grid==1 & plotIDs==0),j,plotIDs)
}</pre> plots <- as.data.frame(plotIDs) names(plots) <- "plotID" plots\$x <- pt.x plots\$y <- pt.y merge(plots,rd,by.x="plotID",by.y="plotID",all.x=T)[,c(2,3,4)] -> plot52
merge(plot52,plots,by.x=c("x","y"),by.y=c("x","y")) -> lu01 write.table(lu01, "phuket5201dig.txt",row.names=F,quote=F) } #-----end of digitization

Figure 10 Program commands for computing digitized land-use

The program contains two sections. The first section removes holes from polygons. This is needed because polygons corresponding to holes are duplicated and are thus redundant, as described in a preceding section. Once their holes have been removed, it is necessary to order the polygons by increasing area, because once the grid-points within a polygon containing a hole have been assigned with a plotID value, they cannot be overwritten. Note that the MID file contains the area of each polygon as one of its fields, but if this information is not available, the area() function can be used to compute the area of a polygon. If the number of grid-points in the whole region is large the program will take much longer, so it is better to spit the whole region into smaller components containing whole polygons and digitize them separately. Note that the *point.in.polygon()* function needs to determine whether or not each specified (x, y) point is inside or outside a polygon specified by its set of boundary points. It does this by computing the number of times a vector originating from the point to a boundary of the region crosses the boundary of the polygon. If this number is odd, the point is inside the polygon; if the number is even, the point is outside the polygon.

# 2.5 Varying the grid density

We used a 100×100 meter grid for digitization, so that each grid point corresponds to one hectare of land. The digitization method can fail to accurately identify small polygons that fall between grid points. However, this problem can be solved by varying the density of the grid where needed. Figure 11 shows an example.



Figure 11. Varying grid for Coral Island containing extra grid-points (right panel)

Table 3: Data structures for 6×5 point rectangle with additional grid-points to

pointID	Х	У	pointID	Х	У	pointID	х	у
2322	431.55	861.25	*397	431.85	860.10	*397	431.85	860.00
2322	431.65	861.25	*397	431.90	860.10	*397	431.90	860.00
401	431.75	861.25	*397	431.95	860.10	*397	431.95	860.00
401	431.85	861.25	*397	432.00	860.10	399	431.55	859.95
401	431.95	861.25	*397	432.05	860.10	*399	431.60	859.95
401	432.05	861.25	399	431.55	860.05	399	431.65	859.95
*397	431.75	861.20	*399	431.60	860.05	401	431.75	859.95
*397	431.80	861.20	399	431.65	860.05	397	431.85	859.95
*397	431.85	861.20	401	431.75	860.05	*397	431.90	859.95
401	431.55	860.15	*397	431.80	860.05	397	431.95	859.95
401	431.65	860.15	397	431.85	860.05	*397	432.00	859.95
401	431.75	860.15	*397	431.90	860.05	401	432.05	859.95
*397	431.80	860.15	397	431.95	860.05	401	431.55	859.85
397	431.85	860.15	*397	432.00	860.05	401	431.65	859.85
*397	431.90	860.15	401	432.05	860.05	401	431.75	859.85
397	431.95	860.15	*399	431.55	860.00	401	431.85	859.85
*397	432.00	860.15	*399	431.60	860.00	401	431.95	859.85
397	432.05	860.15	*399	431.65	860.00	401	432.05	859.85
*397	431.80	860.10	*397	431.80	860.00			

improve accuracy in small polygons (asterisked)

# 2.6 Graphical display

We have seen how thematic maps are appropriate for displaying land-use data defined as polygons. While thematic maps can also be created from digitized data, if the grid is too coarse these maps will be less informative than corresponding maps based on polygons. Other relevant graphical displays include bubble plots, bar charts and plots of confidence intervals. Land-use change for two given years can be graphed as thematic map combined with a bubble plot as shown in Figure 12.



Figure 12. Geographical display showing land-use change in Coral Island

from 2000 to 2009

Graphing land-use change is complicated because many additional colours are needed to illustrate the data from a cross-tabulation that has more than a small number of land-use categories. However, analysis of such change can be simplified by focusing on a binary outcome, such as a specific land-use of interest, such as "developed" land.

#### 2.7 Logistic regression

Logistic regression is an appropriate method for analyzing remote sensing (RS) data where the outcome is binary, such as urban land. This model parameterizes a linear relationship between a set of independent variables and the binary variable using a logit link function, which constrains values of the probability associated with the specific outcome to be between 0 and 1 (Lee and Pradhan, 2007).

This model can be used to handle as independent variables both continuous and categorical predictor variables. Also, these predictors need not have normal distributions as required in discriminant analysis (Ohlmacher and Davis, 2003). Logistic regression coefficients can be used to estimate odds ratios for each of the independent variables in the model (Kundu *et al.*, 2013). For *p* numeric predictor variables  $X_1, X_2, ..., X_p$  the model is formulated as follows (Kleinbaum, 1994).

logit ( 
$$prob[Y_i = 1 | X_1 = x_{i1}, X_2 = x_{i2}, ..., X_p = x_{ip}) = \alpha_i + \sum_{j=1}^p \beta_j x_{ij}$$
 (4)

In this equation  $x_{i1}, x_{i2}, ..., x_{ip}$  are the observed values of  $X_1, X_2, ..., X_p$  for case *i*. For a single categorical (factor) predictor variable *W*, say, this model takes the form

logit ( 
$$prob[Y_i = 1 | \boldsymbol{W}_i = \boldsymbol{w}_i]$$
) =  $\alpha_i + \sum_{j=2}^p \beta_j w_{ij}$ , (5)

where the  $w_{ij}$ , j = 1, 2, ..., p are indicator variables taking binary values 0 or 1. Note that  $w_{i1}$  is omitted from the model because when the intercept term  $\alpha_i$  is included one of the factor levels must be omitted to avoid over-parameterization. For example, if W is land-use with three categories corresponding to forest, agriculture or urban landuse, for case *i*,  $w_{i1}$  is 1 for forest and 0 for other use,  $w_{i2}$  is 1 for agriculture and 0 other use, and  $w_{i3}$  is 1 for urban and 0 for other use.

For analyzing land-use change in the simple situation where no covariates are considered, the binary dependent variable *Y* denotes the specified binary land-use for each grid-point in a specified year, and *X* is the land-use type (not necessarily binary) at the same grid-point for a preceding year. We now show how the logistic regression model is applied to the data for Coral Island, where the binary outcome is Rubber Plantation or other land-use in year 2009 and the predictor is the land-use (Rubber Plantation, Coconut, or other Forest) in year 2000. First, we choose the small sample containing just 30 grid-points as indicated in Figure 12. Since both the outcome variable *Y* and the predictor variable W is categorical, the data to be fitted by the logistic regression model may be listed simply as a contingency table of counts, as shown in the left side of Figure 13. Using a logistic regression program with lu2000 as the predictor and rubber2009/other2009 as the binary outcome, we get the result shown in the right side of Figure 13.

			Coefficient	S:			
lu2000	Rubber2009	Other2009	18.07% ST 10.08%	Estimate Std	. Error	z value	Pr(> z )
			(Intercept)	1.946	1.069	1.820	0.06872 .
Rubber A302	7	1	lu43.A405	-4.025	1.506	-2.673	0.00752 **
Rabberthooz			lu43.F101	-1.476	1.212	-1.218	0.22315
Coconut.A405	1	8	5.7.5				
Forest.F101	8	5	Null de Residual de	viance: 11.8 viance:	25 on 2 0 on 0	degree	s of freedom s of freedom
		1	nesidadi ac	viunee.	o on o	deBi ce	5 of freedom

Figure 13. Data for small sample of 30 grid-points (30 hectares) selected from Figure

12 and result from fitting logistic regression model

Note that the estimate for the predictor level Rubber.A302 is 0 because this parameter is absorbed by the intercept as indicated in Equation (5), and the coefficients and corresponding standard errors and p-values denote the differences from this omitted category. Thus the result shows that coconut was very likely to change to rubber (pvalue for no change 0.0075), but there was no evidence that forest changed to rubber. These results are consistent with the maps in the right panels of Figure 12.

The left panel of Figure 14 depicts a bar chart of the data in the left side of Figure 13. It shows that 77.5% of land devoted to rubber plantation in 2000 remained rubber plantation in 2009, whereas 10% and 61.5% of the land that was coconut and forest, respectively, in 2000 became rubber plantation in 2009.



Figure 14. Bar chart of percentages of land that changed to rubber plantation in a sample of 30 hectares in Coral island from 2000 to 2009, with 95% confidence intervals for comparing them (right panel)

It was not necessary to use the logistic regression method just to get these percentages because they are obtained simply from the table on the left of Figure 13. However, the logistic regression model is needed because it also provides standard errors for these percentages, based on the assumption that the 30 hectare area is a subset from a larger population from which the 30 hectares is a randomly selected sample. These standard errors can be used to construct 95% confidence intervals for comparing the population percentages, and these are superimposed on the bar chart on the right side of Figure 14. They show that the population percentages for the changes from coconut and forest to rubber differed. This conclusion is consistent with the p-value 0.0075 shown in the logistic regression result on the right side of Figure 13, which shows evidence that the percentage of coconut land that changed to rubber was less than the percentage of rubber that remained rubber.

When analyzing land-use change from an earlier survey year to a later year it is important to ensure that the samples are taken from the same area. However, with shifting coordinates and changes in coastlines it can happen that these areas are not exactly the same. For example, the land area of Coral Island in 2000 was reportedly 440 hectares and 434 hectares in 2009, and its total land area that did not change was 424 hectares. So analyzing land-use change, we consider only this common area. Figure 15 shows the data and results from fitting the same model to the common area of Coral Island as before for the smaller sample of just 30 hectares.



Figure 15. Data for Coral Island (424 hectares) and fitted logistic regression model Since location is an important predictor of land-use change, next we give a simple illustration of how the logistic regression model can be extended to include this addition predictor, by dividing Coral Island into two sections, one west of UTM 430.5 km East and the other east of this longitude. Taking the combination of land-use in 2000 and this east/west location as a single factor, Figure 16 shows the result of fitting the logistic model, which computed by program commands in appendix.



Figure 16. Data for Coral Island (424 hectares), which separated to west and east and fitted logistic regression model

#### 2.8 Adjusting for spatial correlation

Conventional statistical analysis such as logistic regression assumes that data samples (*Y*) are independent. However, this assumption does not hold for data defined at gridpoints (raster) just 100 meters apart. The data from neighboring plots are likely to be mutually correlated, violating the independence assumption, giving incorrect standard errors. Previous studies with geographical data such as those by McNeil and Chooprateep (2013) handled spatial correlation by aggregating data in larger regions with acceptably small correlation between overlapping regions, or used factor analysis to adjust for these correlations. The generalized estimating equations (GEE) method could be used by dividing the region into groups of plots (clusters) and estimating common fixed correlations between plots in the same group (Zeger and Liang 1986).

However, this method assumes a single common correlation, whereas it is likely that the spatial correlation in land-use data will vary with the type of land-use. For binary outcomes a simpler method is available, based on variation inflation factors, proposed by Rao and Scott (1992). This method avoids the problem in the GEE method by computing effective sample sizes for sets of land-use plots based on their sample variances, and then expanding the confidence intervals given by the logistic regression model by multiplying them by the square roots of these factors.

