

## **APPENDIX A**

### **CALCULATION OF THE MOLECULAR WEIGHT OF MCPO**

**Main fatty acid of MCPO (Table 2.2)**

Palmitic acid = 47 %wt      Oleic acid = 43 %wt      Linoleic acid = 10 %wt

**Calculation of molecular weight of TG**

Molecular weight of TG (Palmitic acid) = 806 g/mol

Molecular weight of TG (Oleic acid) = 884 g/mol

Molecular weight of TG (Linoleic acid) = 878 g/mol

Average of molecular weight of TG =  $(806 \times 0.47) + (884 \times 0.43) + (878 \times 0.10)$   
 = 846.64 g/mol

**Calculation of molecular weight of DG**

Molecular weight of DG (Palmitic acid) = 568 g/mol

Molecular weight of DG (Oleic acid) = 620 g/mol

Molecular weight of DG (Linoleic acid) = 616 g/mol

Average of molecular weight of DG =  $(568 \times 0.47) + (620 \times 0.43) + (616 \times 0.10)$   
 = 595.16 g/mol

**Calculation of molecular weight of MG**

Molecular weight of MG (Palmitic acid) = 318 g/mol

Molecular weight of MG (Oleic acid) = 356 g/mol

Molecular weight of MG (Linoleic acid) = 354 g/mol

Average of molecular weight of MG =  $(318 \times 0.47) + (356 \times 0.43) + (354 \times 0.10)$   
 = 338.04 g/mol

### Calculation of molecular weight of FFA

$$\text{Molecular weight of FFA (Palmitic acid)} = 256 \text{ g/mol}$$

$$\text{Molecular weight of FFA (Oleic acid)} = 282 \text{ g/mol}$$

$$\text{Molecular weight of FFA (Linoleic acid)} = 280 \text{ g/mol}$$

$$\begin{aligned} \text{Average of molecular weight of FFA} &= (256 \times 0.47) + (282 \times 0.43) + (280 \times 0.10) \\ &= 269.58 \text{ g/mol} \end{aligned}$$

### Calculation of molecular weight of ME

$$\text{Molecular weight of ME (Palmitic acid)} = 270 \text{ g/mol}$$

$$\text{Molecular weight of ME (Oleic acid)} = 296 \text{ g/mol}$$

$$\text{Molecular weight of ME (Linoleic acid)} = 294 \text{ g/mol}$$

$$\begin{aligned} \text{Average of molecular weight of ME} &= (270 \times 0.47) + (296 \times 0.43) + (294 \times 0.10) \\ &= 283.58 \text{ g/mol} \end{aligned}$$

**Table A.1** The concentration of compounds in MCPO from analysis using standard methods

Analytic Method	The concentration of compounds in MCPO (%wt)				
	TG	DG	MG	FFA	ME
Standard Method*	82.068	8.823	0.204	8.632	0.274

\*Source from Figure E.2, E.3, and E.4

### Calculation of molecular weight of MCPO by Standard Method

$$\begin{aligned} \text{Molecular weight of MCPO} &= (846.64 \times 0.821) + (595.16 \times 0.088) + \\ &\quad (338.04 \times 0.002) + (269.58 \times 0.086) + \\ &\quad (283.58 \times 0.003) \\ &= 772.065 \text{ g/mol} \# \end{aligned}$$

**APPENDIX B**  
**KARL FISCHER ANALYSIS**

Karl Fisher

The first-stage samples were analyzed for water by Karl Fisher. The weighed commercial methanol was added in the weighed samples and shaken. Then the solutions were released for separating the oily solution and clear solution. After that, the clear solution, which was drawn and weighed, was analyzed for the amount of water with Karl Fisher. The mass ratio of water was determined and then calculated the real mass ratio of water in each sample.

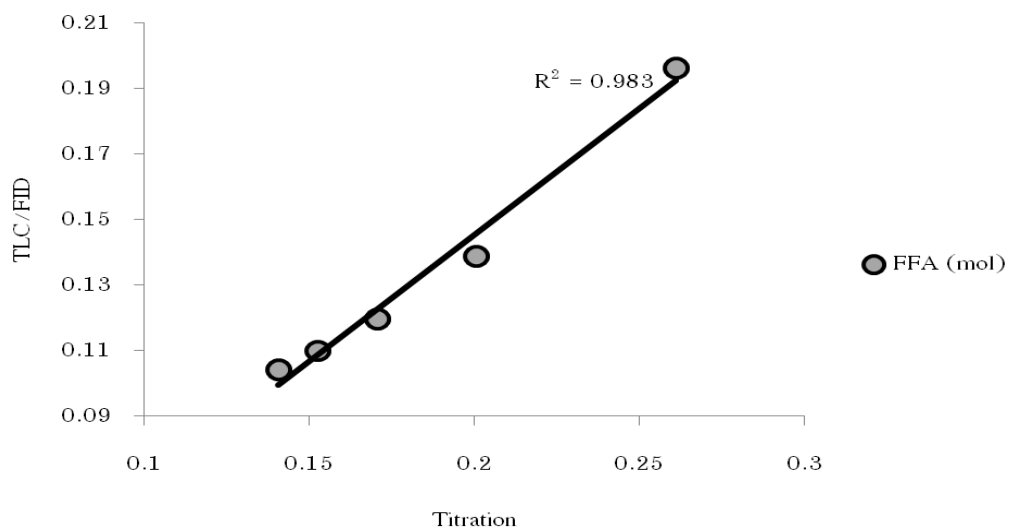
Example: What is the concentration of water in CPO (0.500 g) when 0.529 %wt is the concentration of water in the clear solution (MeOH) (2.420g) with 0.100 %wt water?

Solve:	Clear solution	100	g has water (solution + MeOH)	0.529	g
	Clear solution	2.420	g has water	0.0128	g
	MeOH	100	g has water	0.100	g
	MeOH	2.420	g has water	0.00242	g

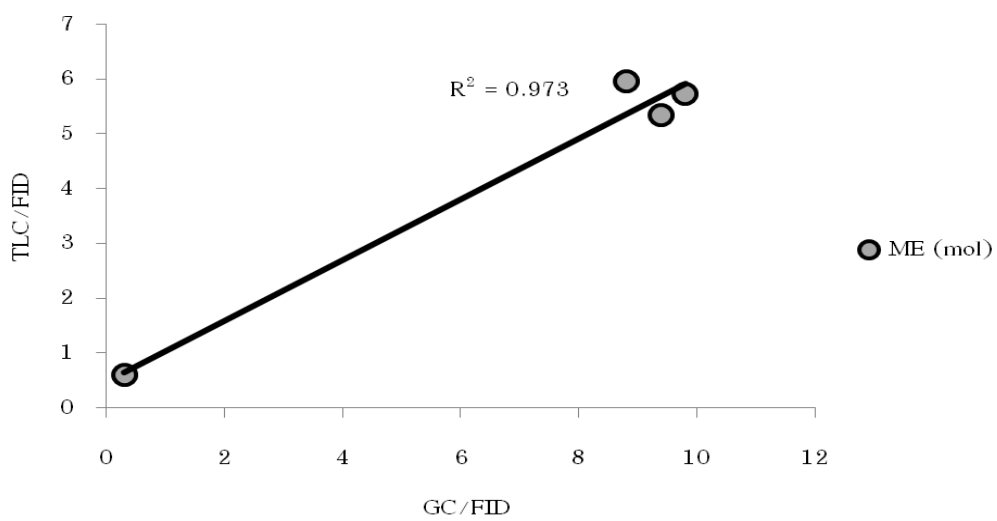
$\therefore$  Clear solution has water  $0.0128 - 0.00242 = 0.01038$  g

Sampling	0.500	g has water	0.01038	g
Sampling	100	g has water	2.0760	g

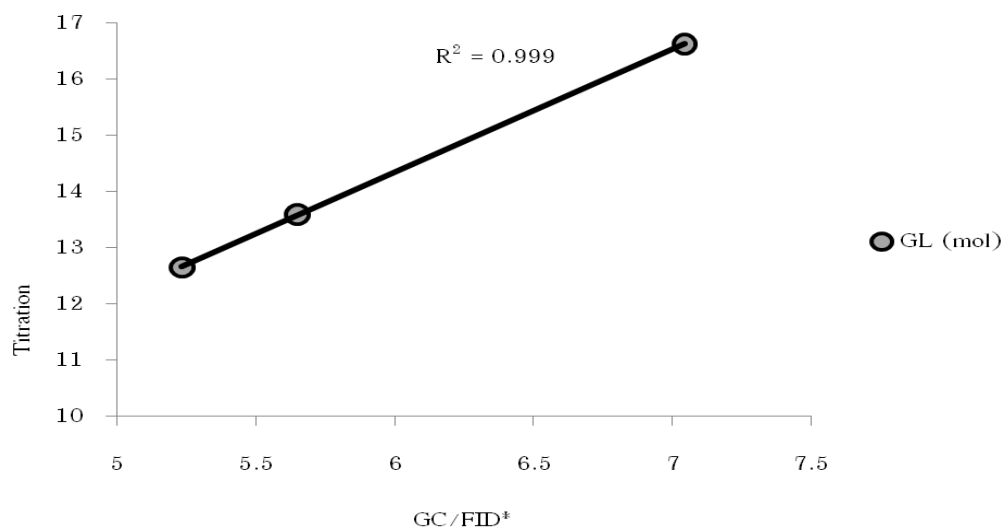
**APPENDIX C**  
**COMPARISON OF ANALYTICAL INSTRUMENT**



**Figure C.1** Comparison of FFA determination between TLC/FID and Titration



**Figure C.2** Comparison of ME determination between TLC/FID and GC/FID



\*GL data from GC/FID tried out by analyst from Science Equipment Center, PSU

**Figure C.3** Comparison of GL determination between Titration and GC/FID



## APPENDIX D

### RAW DATA FOR THE TWO-STAGE PROCESS

Table with 5 columns and approximately 15 rows of data. The text is extremely faint and illegible.

**Table D.1** FFA conversion in MCPO by using a 1:1 molar ratio of methanol to oil at a temperature of 55 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without water (%wt)	TG without water (%wt)	FFA without water (%wt)	DG without water (%wt)	MG without water (%wt)	WT (%wt)
0	1.832	2	1.584	82.722	11.057	4.218	0.119	0.079
0.5	1.824	2	8.019	77.653	4.564	9.074	0.690	0.481
1	1.820	2	9.271	77.416	3.286	9.111	0.916	0.464
3	1.820	2	8.350	80.249	2.704	7.943	0.755	0.584
5	1.812	2	10.120	78.091	1.749	9.207	0.832	0.607
7	1.818	2	8.188	80.690	2.327	8.143	0.652	0.573
9	1.810	2	7.680	83.647	1.564	5.961	1.149	0.461
12	1.816	2	9.857	78.888	2.061	8.394	0.801	0.493
15	1.822	2	8.432	80.171	2.467	8.241	0.690	0.590
20	1.810	2	9.885	79.078	1.885	8.349	0.802	0.692

**Table D.2** FFA conversion in MCPO by using a 1:1 molar ratio of methanol to oil at a temperature of 60 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without water (%wt)	TG without water (%wt)	FFA without water (%wt)	DG without water (%wt)	MG without water (%wt)	WT (%wt)
0	1.832	2	1.282	83.710	10.328	4.523	0.157	0.064
0.5	1.828	2	3.982	83.354	5.489	6.699	0.475	0.319
1	1.824	2	5.916	81.650	4.604	7.335	0.494	0.473
3	1.820	2	6.336	86.333	2.164	4.806	0.361	0.507
5	1.812	2	3.759	89.637	1.585	4.641	0.378	0.301
7	1.812	2	4.856	88.817	1.229	4.688	0.410	0.388
9	1.816	2	4.301	89.777	1.327	4.318	0.277	0.344
12	1.810	2	6.956	84.392	2.532	5.851	0.270	0.556
15	1.808	2	7.122	81.567	2.659	6.888	0.383	0.570
20	1.812	2	7.690	83.930	2.659	5.318	0.403	0.615

**Table D.3** FFA conversion in MCPO by using a 1:1 molar ratio of methanol to oil at a temperature of 65 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without water (%wt)	TG without water (%wt)	FFA without water (%wt)	DG without water (%wt)	MG without water (%wt)	WT (%wt)
0	1.832	2	1.774	83.159	10.057	4.361	1.047	0.089
0.5	1.82	2	7.718	82.583	1.900	6.990	0.810	0.540
1	1.812	2	9.687	79.619	1.601	8.071	1.024	0.678
3	1.8	2	5.178	84.936	1.599	7.686	0.603	0.362
5	1.81	2	6.674	82.275	1.685	8.255	1.110	0.467
7	1.81	2	5.865	78.316	1.669	9.757	4.394	0.411
9	1.802	2	8.235	78.959	1.193	10.133	0.481	0.576
12	1.816	2	8.746	78.026	1.218	10.134	0.978	0.612
15	1.812	2	9.846	77.318	1.228	10.991	0.618	0.689
20	1.78	2	10.612	77.726	0.973	9.731	0.958	0.743

**Table D.4** FFA conversion in MCPO by using a 2.5:1 molar ratio of methanol to oil at a temperature of 55 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without water (%wt)	TG without water (%wt)	FFA without water (%wt)	DG without water (%wt)	MG without water (%wt)	WT (%wt)
0	1.832	2	0.000	86.809	11.957	4.013	0.941	0.080
0.5	1.808	2	6.508	85.316	1.381	6.200	0.597	0.390
1	1.798	2	6.646	86.332	0.945	5.853	0.525	0.332
3	1.790	2	6.483	86.208	0.881	5.995	0.633	0.454
5	1.800	2	7.061	84.103	0.905	7.590	0.342	0.424
7	1.804	2	6.704	87.089	1.169	5.088	0.551	0.469
9	1.802	2	9.540	79.984	1.308	8.321	0.848	0.572
12	1.794	2	9.427	76.373	1.204	11.424	1.174	0.471
15	1.798	2	8.629	83.985	1.317	6.459	0.600	0.604
20	1.788	2	6.970	84.850	1.117	6.548	0.515	0.488

**Table D.5** FFA conversion in MCPO by using a 2.5:1 molar ratio of methanol to oil at a temperature of 60 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without water (%wt)	TG without water (%wt)	FFA without water (%wt)	DG without water (%wt)	MG without water (%wt)	WT (%wt)
0	1.832	2	1.564	83.290	10.559	4.585	0.541	0.098
0.5	1.788	2	8.438	83.223	0.828	6.413	1.698	0.422
1	1.794	2	7.793	85.696	0.687	5.633	0.192	0.468
3	1.802	2	9.426	85.400	0.864	6.784	0.427	0.613
5	1.782	2	9.940	79.539	0.526	9.555	0.541	0.646
7	1.792	2	10.850	77.700	0.470	8.615	1.368	0.543
9	1.794	2	10.335	77.216	0.637	9.407	0.506	0.517
12	1.790	2	10.718	77.167	0.415	10.173	0.529	0.643
15	1.786	2	10.286	76.854	0.551	10.417	0.493	0.514
20	1.784	2	12.316	75.509	0.817	10.986	0.374	0.616

**Table D.6** FFA conversion in MCPO by using a 2.5:1 molar ratio of methanol to oil at a temperature of 65 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without water (%wt)	TG without water (%wt)	FFA without water (%wt)	DG without water (%wt)	MG without water (%wt)	WT (%wt)
0	1.832	2	1.473	84.891	11.559	4.065	1.069	0.074
0.5	1.788	2	9.298	82.887	0.677	6.295	0.844	0.465
1	1.794	2	8.576	84.886	0.449	5.660	0.430	0.515
3	1.798	2	9.851	83.541	0.671	5.222	0.716	0.542
5	1.782	2	9.844	82.076	0.531	6.830	0.521	0.541
7	1.78	2	10.366	82.903	0.118	4.282	1.333	0.570
9	1.794	2	8.042	84.931	0.332	6.396	0.301	0.563
12	1.79	2	8.810	80.036	0.574	9.394	0.987	0.529
15	1.792	2	9.906	81.941	0.498	6.512	0.335	0.799
20	1.782	2	7.749	84.211	0.593	6.022	0.848	0.585

**Table D.7** FFA conversion in MCPO by using a 3.5:1 molar ratio of methanol to oil at a temperature of 55 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without water (%wt)	TG without water (%wt)	FFA without water (%wt)	DG without water (%wt)	MG without water (%wt)	WT (%wt)
0	1.832	2	1.864	85.345	10.038	3.592	0.160	0.093
0.5	1.788	2	7.843	85.608	0.601	5.999	0.150	0.549
1	1.794	2	9.273	84.181	0.261	6.175	0.110	0.649
3	1.790	2	8.363	85.586	0.153	5.806	0.092	0.585
5	1.786	2	10.206	83.152	0.200	5.683	0.161	0.714
7	1.786	2	9.161	83.856	0.357	6.404	0.123	0.641
9	1.784	2	10.683	82.435	0.211	6.616	0.057	0.748
12	1.794	2	10.074	84.251	0.256	5.319	0.099	0.705
15	1.796	2	10.395	84.272	0.221	5.077	0.106	0.728
20	1.784	2	7.949	86.632	0.080	5.250	0.089	0.556

**Table D.8** FFA conversion in MCPO by using a 3.5:1 molar ratio of methanol to oil at a temperature of 60 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without water (%wt)	TG without water (%wt)	FFA without water (%wt)	DG without water (%wt)	MG without water (%wt)	WT (%wt)
0	1.832	2	1.864	83.290	9.820	4.585	0.441	0.098
0.5	1.780	2	8.642	82.320	0.283	8.416	0.349	0.588
1	1.782	2	10.985	82.797	0.130	4.817	0.272	0.604
3	1.780	2	9.388	85.120	0.130	4.504	0.860	0.610
5	1.788	2	10.145	83.078	0.053	6.530	0.195	0.710
7	1.782	2	7.349	88.660	0.000	3.549	0.444	0.514
9	1.786	2	9.436	84.419	0.131	6.336	0.180	0.613
12	1.780	2	8.994	80.634	0.080	9.387	0.208	0.630
15	1.790	2	9.318	84.255	0.091	4.779	0.763	0.606
20	1.784	2	9.318	84.804	0.000	5.281	0.598	0.652

**Table D.9** FFA conversion in MCPO by using a 3.5:1 molar ratio of methanol to oil at a temperature of 65 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without water (%wt)	TG without water (%wt)	FFA without water (%wt)	DG without water (%wt)	MG without water (%wt)	WT (%wt)
0	1.832	2	1.133	84.530	9.627	4.584	0.279	0.057
0.5	1.782	2	9.089	83.520	0.923	6.226	1.166	0.591
1	1.784	2	7.558	84.513	0.295	6.137	1.499	0.605
3	1.780	2	7.647	85.453	0.125	5.990	0.786	0.612
5	1.786	2	9.584	88.982	0.135	5.753	0.546	0.719
7	1.782	2	8.714	82.233	0.302	7.986	0.566	0.654
9	1.780	2	10.239	81.140	0.294	7.712	0.616	0.717
12	1.780	2	9.300	81.498	0.141	8.394	0.269	0.698
15	1.782	2	9.188	78.930	0.223	10.454	0.392	0.735
20	1.786	2	7.690	80.359	0.923	8.297	0.993	0.754

**Table D.10** ME conversion in MCPO by using a 2.5:1 molar ratio of methanol to oil at a temperature of 55 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without GL (%wt)	TG without GL (%wt)	DG without GL (%wt)	MG without GL (%wt)	GL (%wt)
0	1.832	2	1.282	7.957	4.623	0.157	0.064
0.5	1.828	2	3.982	83.354	6.699	0.475	0.319
1	1.824	2	5.916	81.650	7.335	0.494	0.473
3	1.820	2	6.336	86.333	4.806	0.361	0.507
5	1.812	2	3.759	89.637	4.641	0.378	0.301
7	1.812	2	4.856	88.817	4.688	0.410	0.388
9	1.816	2	4.301	89.777	4.318	0.277	0.344
12	1.810	2	6.956	84.392	5.851	0.270	0.556
15	1.808	2	7.122	81.567	6.888	0.383	0.570
20	1.812	2	7.690	83.930	5.318	0.403	0.615

**Table D.11** ME conversion in MCPO by using a 2.5:1 molar ratio of methanol to oil at a temperature of 60 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without GL (%wt)	TG without GL (%wt)	DG without GL (%wt)	MG without GL (%wt)	GL (%wt)
0	1.832	2	1.282	7.957	4.623	0.157	0.064
0.5	1.828	2	3.982	83.354	6.699	0.475	0.319
1	1.824	2	5.916	81.650	7.335	0.494	0.473
3	1.820	2	6.336	86.333	4.806	0.361	0.507
5	1.812	2	3.759	89.637	4.641	0.378	0.301
7	1.812	2	4.856	88.817	4.688	0.410	0.388
9	1.816	2	4.301	89.777	4.318	0.277	0.344
12	1.810	2	6.956	84.392	5.851	0.270	0.556
15	1.808	2	7.122	81.567	6.888	0.383	0.570
20	1.812	2	7.690	83.930	5.318	0.403	0.615

**Table D.12** ME conversion in MCPO by using a 2.5:1 molar ratio of methanol to oil at a temperature of 65 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without GL (%wt)	TG without GL (%wt)	DG without GL (%wt)	MG without GL (%wt)	GL (%wt)
0	1.832	2	1.282	7.957	4.623	0.157	0.064
0.5	1.828	2	3.982	83.354	6.699	0.475	0.319
1	1.824	2	5.916	81.650	7.335	0.494	0.473
3	1.820	2	6.336	86.333	4.806	0.361	0.507
5	1.812	2	3.759	89.637	4.641	0.378	0.301
7	1.812	2	4.856	88.817	4.688	0.410	0.388
9	1.816	2	4.301	89.777	4.318	0.277	0.344
12	1.810	2	6.956	84.392	5.851	0.270	0.556
15	1.808	2	7.122	81.567	6.888	0.383	0.570
20	1.812	2	7.690	83.930	5.318	0.403	0.615

**Table D.13** ME conversion in MCPO by using a 5:1 molar ratio of methanol to oil at a temperature of 55 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without GL (%wt)	TG without GL (%wt)	DG without GL (%wt)	MG without GL (%wt)	GL (%wt)
0	1.832	2	1.282	7.957	4.623	0.157	0.064
0.5	1.828	2	3.982	83.354	6.699	0.475	0.319
1	1.824	2	5.916	81.650	7.335	0.494	0.473
3	1.820	2	6.336	86.333	4.806	0.361	0.507
5	1.812	2	3.759	89.637	4.641	0.378	0.301
7	1.812	2	4.856	88.817	4.688	0.410	0.388
9	1.816	2	4.301	89.777	4.318	0.277	0.344
12	1.810	2	6.956	84.392	5.851	0.270	0.556
15	1.808	2	7.122	81.567	6.888	0.383	0.570
20	1.812	2	7.690	83.930	5.318	0.403	0.615

**Table D.14** ME conversion in MCPO by using a 5:1 molar ratio of methanol to oil at a temperature of 60 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without GL (%wt)	TG without GL (%wt)	DG without GL (%wt)	MG without GL (%wt)	GL (%wt)
0	1.832	2	1.282	7.957	4.623	0.157	0.064
0.5	1.828	2	3.982	83.354	6.699	0.475	0.319
1	1.824	2	5.916	81.650	7.335	0.494	0.473
3	1.820	2	6.336	86.333	4.806	0.361	0.507
5	1.812	2	3.759	89.637	4.641	0.378	0.301
7	1.812	2	4.856	88.817	4.688	0.410	0.388
9	1.816	2	4.301	89.777	4.318	0.277	0.344
12	1.810	2	6.956	84.392	5.851	0.270	0.556
15	1.808	2	7.122	81.567	6.888	0.383	0.570
20	1.812	2	7.690	83.930	5.318	0.403	0.615

**Table D.15** ME conversion in MCPO by using a 5:1 molar ratio of methanol to oil at a temperature of 65 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without GL (%wt)	TG without GL (%wt)	DG without GL (%wt)	MG without GL (%wt)	GL (%wt)
0	1.832	2	1.282	7.957	4.623	0.157	0.064
0.5	1.828	2	3.982	83.354	6.699	0.475	0.319
1	1.824	2	5.916	81.650	7.335	0.494	0.473
3	1.820	2	6.336	86.333	4.806	0.361	0.507
5	1.812	2	3.759	89.637	4.641	0.378	0.301
7	1.812	2	4.856	88.817	4.688	0.410	0.388
9	1.816	2	4.301	89.777	4.318	0.277	0.344
12	1.810	2	6.956	84.392	5.851	0.270	0.556
15	1.808	2	7.122	81.567	6.888	0.383	0.570
20	1.812	2	7.690	83.930	5.318	0.403	0.615

**Table D.16** ME conversion in MCPO by using a 7.5:1 molar ratio of methanol to oil at a temperature of 55 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without GL (%wt)	TG without GL (%wt)	DG without GL (%wt)	MG without GL (%wt)	GL (%wt)
0	1.832	2	1.282	7.957	4.623	0.157	0.064
0.5	1.828	2	3.982	83.354	6.699	0.475	0.319
1	1.824	2	5.916	81.650	7.335	0.494	0.473
3	1.820	2	6.336	86.333	4.806	0.361	0.507
5	1.812	2	3.759	89.637	4.641	0.378	0.301
7	1.812	2	4.856	88.817	4.688	0.410	0.388
9	1.816	2	4.301	89.777	4.318	0.277	0.344
12	1.810	2	6.956	84.392	5.851	0.270	0.556
15	1.808	2	7.122	81.567	6.888	0.383	0.570
20	1.812	2	7.690	83.930	5.318	0.403	0.615

**Table D.17** ME conversion in MCPO by using a 7.5:1 molar ratio of methanol to oil at a temperature of 60 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without GL (%wt)	TG without GL (%wt)	DG without GL (%wt)	MG without GL (%wt)	GL (%wt)
0	1.832	2	1.282	7.957	4.623	0.157	0.064
0.5	1.828	2	3.982	83.354	6.699	0.475	0.319
1	1.824	2	5.916	81.650	7.335	0.494	0.473
3	1.820	2	6.336	86.333	4.806	0.361	0.507
5	1.812	2	3.759	89.637	4.641	0.378	0.301
7	1.812	2	4.856	88.817	4.688	0.410	0.388
9	1.816	2	4.301	89.777	4.318	0.277	0.344
12	1.810	2	6.956	84.392	5.851	0.270	0.556
15	1.808	2	7.122	81.567	6.888	0.383	0.570
20	1.812	2	7.690	83.930	5.318	0.403	0.615

**Table D.18** ME conversion in MCPO by using a 7.5:1 molar ratio of methanol to oil at a temperature of 65 degree Celsius

Time (min)	Weight (g)	Volume (cm <sup>3</sup> )	ME without GL (%wt)	TG without GL (%wt)	DG without GL (%wt)	MG without GL (%wt)	GL (%wt)
0	1.832	2	1.282	7.957	4.623	0.157	0.064
0.5	1.828	2	3.982	83.354	6.699	0.475	0.319
1	1.824	2	5.916	81.650	7.335	0.494	0.473
3	1.820	2	6.336	86.333	4.806	0.361	0.507
5	1.812	2	3.759	89.637	4.641	0.378	0.301
7	1.812	2	4.856	88.817	4.688	0.410	0.388
9	1.816	2	4.301	89.777	4.318	0.277	0.344
12	1.810	2	6.956	84.392	5.851	0.270	0.556
15	1.808	2	7.122	81.567	6.888	0.383	0.570
20	1.812	2	7.690	83.930	5.318	0.403	0.615

**APPENDIX E**

**ANALYTICAL DATA FOR THE TWO-STAGE PROCESS**





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No. 8177/49 Page1/1

## TEST REPORT

**Client Name and Address :** Mr. Surachai Jansri  
 Department of Mechanical Engineering, Faculty of Engineering,  
 Prince of Songkla University

**Test Request Form No.:** 9560/49 (refer to Test Request Form No. 8619/49 received date May 22, 2006)

**Test item(s) received date :** September 27, 2006

**Analyst :** Miss Sathida Malee

**Test performed date :** May 23, 2006

**Test Method used :** Refer to EN 14110:2003

**Test Instrument :** HP 6850 Gas Chromatograph with Flame Ionization Detector

**Test Technique:** Head Space-Gas Chromatography

**Test Condition :** Inlet temperature: 150°C  
 Oven temperature: 50°C 5 minutes  
 Detector temperature: 150°C  
 Column: Innowax , length 30 m., 250 µm I.D, 0.25 µm film thickness

**Test item(s) description :** Biodiesel from CPO **Quantity :** 3 Samples

**Test Results :**

No.	Sample	Methanol content ± standard deviation, %
1	V1 check CH <sub>3</sub> OH	42.49 ± 0.49
2	V2 check CH <sub>3</sub> OH	32.68 ± 3.03
3	V3 check CH <sub>3</sub> OH	44.26 ± 0.36

LOQ of Methanol = 0.01%

Refer to Folder 8619-49

(Miss Patchara Sukonrat)

Inspector

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Figure E.1 Remained methanol content in the first stage solution



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**TEST REPORT**

**Client Name and Address :** Mr. Surachai Jansri  
 Department of Mechanical Engineering, Faculty of Engineering  
 Prince of Songkla University

**Test Request Form No.:** 10245/49

**Test item(s) received date :** December 29, 2006

**Analyst :** Miss Pimpimol Penjamras

**Test performed date :** December 29, 2006

**Test Method used :** Refer to WI-RES- GC-001

**Test Instrument :** Agilent 6890 Gas Chromatograph with Flame Ionization Detector

**Test Technique:** Gas Chromatography

**Test Condition :** Gas Chromatograph

Inlet temperature: 250 °C Detector temperature: 300 °C  
 Oven initial temperature: 210 °C 30 minutes Hydrogen flow: 30 ml/min  
 Ramp to 250 °C 1 minute at 20 °C / minute Air flow: 300 ml/min  
 Column:HP-INNOWAX, 30 m., film thickness 0.25µm, ID. 0.25 mm Makeup flow: 25 ml/min

**Test item(s) description :** - **Quantity :** 4 Samples

**Test Results :**

No.	Sample name	The % wt. of	
		ester content (C), (SD)	linolenic acid methyl ester content (L), (SD)
1	MCPO	0.3, (0.009)	0.0
2	Esterification 5 min	8.8, (0.035)	0.4, (0.0006)
3	Esterification 10 min	9.8, (0.022)	0.4, (0.018)
4	Esterification 20 min	9.4, (0.066)	0.4, (0.008)

Refer to folder 9931\_49

(Ms. Patchara Sukonrat)  
 Inspector

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**Figure E.2** Ester content of first-stage process at different times



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No.8561/49 Page 1/1

### TEST REPORT

**Client Name and Address :** Mr. Surachai Jansri  
 Department of Mechanical Engineering, Faculty of Engineering,  
 Prince of Songkla University

**Test Request Form No.:** 9932/49

**Test item(s) received date :** November 23, 2006

**Analyst :** Miss Pimpimol Penjamras

**Test performed date :** November 30, 2006

**Test Method used :** Refer to REF-RES-Wetlab-004

**Test Instrument :** -

**Test Technique:** Free fatty acid : Titrimetric Method

**Test Condition :** -

**Test item(s) description :** Crude palm oil **Quantity :** 1 Sample

**Test Results :**

Sample name	Free fatty acid value,(SD)
MCPO	9.4 mgKOH/ g, (0.1)

(Ms. Patchara Sukonrat)

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**Figure E.3** Free fatty acid value of MCPO



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สำเนา

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No. 0291/50 Page1/1

**TEST REPORT**

**Client Name and Address :** Mr. Surachai Jansri  
 Department of Mechanical Engineering, Faculty of Engineering,  
 Prince of Songkla University

**Test Request Form No.:** 0096/50

**Test item(s) received date :** January 10, 2007

**Analyst :** Miss Sathida Malee

**Test performed date :** January 24-25, 2007

**Test Method used :** Refer to EN 14105:2003

**Test Instrument :** HP 6890 Gas Chromatograph with Flame Ionization Detector

**Test Technique:** Gas Chromatography

**Test Condition :** Inlet temperature: Track oven                      Detector temperature: 380°C  
 Oven initial temperature: 50°C, hold 1 minute  
 Ramp to : 180 ° C , at 15°C / minute  
 Ramp to : 230 ° C , at 7 ° C / minute  
 Ramp to : 370 ° C , at 10 ° C / minute, hold 5 minutes  
 Column: DB-5HT , length 15 m., 320 µm I.D, 0.1 µm film thickness plus  
 Retention gap, length 5 m., 320 µm I.D

**Test item(s) description :** Oil and glycerol                      **Quantity :** 1 Sample

**Test Results :**

Sample	Content (%RSD), %		
	Monoglyceride	Diglyceride	Triglyceride
MCPO	0.237 (0.994)	10.276 (1.217)	95.587 (0.738)

*Patchara Sukonrat*

(Miss Patchara Sukonrat)

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Figure E.4 MG, DG and TG content in MCPO



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**TEST REPORT**

**Client Name and Address :** Mr. Surachai Jansri  
 Department of Mechanical Engineering, Faculty of Engineering  
 Prince of Songkla University

**Test Request Form No.:** 1314/50

**Test item(s) received date :** May 21, 2007

**Analyst :** Miss Pimpimol Penjamras

**Test performed date :** May 24-26, 2007

**Test Method used :** Refer to WI-RES- GC-001

**Test Instrument :** Agilent 6890 Gas Chromatograph with Flame Ionization Detector

**Test Technique:** Gas Chromatography

**Test Condition :** **Gas Chromatograph**

Inlet temperature: 250 °C	Detector temperature: 300 °C
Oven initial temperature: 50 °C 2 minutes	Hydrogen flow: 30 ml/min
Ramp to 250 °C 7 minute at 10 °C / minute	Air flow: 300 ml/min
Column:HP-INNOWAX, 30 m., film thickness 0.25µm, ID. 0.25 mm	Makeup flow: 25 ml/min

**Test item(s) description :** Biodiesel (B100)   **Quantity :** 1    Sample

**Test Results :**

Sample name	The % wt. of	
	The % ester C content, (SD)	The % Linolenic acid methyl ester content, (SD)
Mix-CPOME	93.2, (0.4)	0.3,(0.003)
Limit range	Minimum 96.5 %	Maximun 12 %

Refer to folder 1314\_50

(Ms. Patchara Sukonrat)  
**Inspector**

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**Figure E.5** The % ester content of biodiesel produce from MCPO



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No. 1082 / 50 Page 1 / 1

**TEST REPORT**

**Client Name and Address :** Mr. Surachai Jansri  
 Department of Mechanical Engineering, Faculty of Engineering, PSU.

**Test Request Form No.:** 1222 / 50 (Refers to F-ASO-022 No. 1146/50, April 30, 2007)

**Test item(s) received date :** May 9, 2007

**Analyst :** Miss Sunaree Bordeepong

**Test performed date :** May 1, 2007

**Test Method used :** Refer to WI-RES-Hydrometer-001, REF-RES-ASTM D1298-99<sup>B2</sup> และ REF-RES-ASTM D 1250-04  
 S/W-RES-Hydrometer-001

**Test Instrument :** Hydrometer

**Test Technique:** -

**Test Condition :** Objective : Density ASTM D1298

**Test item(s) description :** Biodiesel (B100) **Quantity :** 1 sample

**Test Result :**

No.	Sample	Density at 15 °C (kg/m <sup>3</sup> )	%RSD
1	MIX-CPOME	878.7	0.02

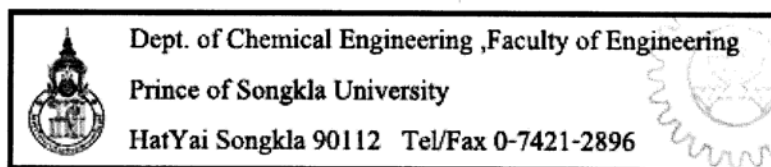
(Miss Patchara Sukonrat)

Inspector

**Remark** This Test report is valid only for the tested sample.

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**Figure E.6** Density of biodiesel prepared from MCPO



Customer: Mr.Surachai Jansri

Department of Mechanical Engineering.

Date : May 1, 2007

Sample : Mix-CPOME

Item	Results
Flash point ( °C )	167
Viscosity @ 40 °C (cSt)	5.28
Copper strip corrosion	No.1a

Analyst : Sorawit Jitbunjerdkul



(Asst.Prof. Pakamas Jespatananon,Ph.D)

**Figure E.7** Flash point and viscosity of biodiesel from MCPO



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**TEST REPORT**

**Client Name and Address :** Mr.Surachai Jansri  
 Department of Mechanical Engineering, Faculty of Engineering, Prince of Songkla University

**Test Request Form No.:** 1149 / 50

**Test item(s) received date :** April 30, 2007

**Analyst :** Ms.Patchara Sukonrat

**Test performed date :** May 4, 2007

**Test Method used :** Refer to WI-RES-XRF-001 and WI-RES-XRF-002

**Test Instrument :** X-ray fluorescence spectrometer (PHILIPS, PW2400)

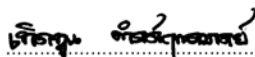
**Test Technique:** X-ray fluorescence spectrometry

**Test Condition :** X-ray tube : Rh tube X-ray path : Helium  
 Application : S in Oil Sample preparation : Liquid cup with 6 $\mu$  polypropylene  
 Objective : S

**Test item(s) description :** Biodiesel (B100) **Quantity :** 1 Sample

**Test Results :**

No.	Sample	Sulphur(%)	RMS
1	Mix-CPOME	0.0004	0.0001



(Mr.Terdtoon Dumrongrittamatt)

Inspector

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**Figure E.8** Sulphur content of biodiesel made from MCPO





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No. 1116/50 Page1/1

### TEST REPORT

**Client Name and Address :** Mr. Surachai Jansri  
Department of Mechanical Engineering, Faculty of Engineering, Prince of Songkla University

**Test Request Form No.:** 1151/50

**Test item(s) received date :** April 30, 2007

**Analyst :** Miss Waraporn Ratsameepakai

**Test performed date :** May 9-14, 2007

**Test Method used :** Refer to REF-ASTM D 874-00

**Test Instrument :** High Temperature Furnace

**Test Technique:** Gravimetric method

**Test Condition :** Ignite at  $775 \pm 25$  °C

**Test item(s) description :** Biodiesel (B100) **Quantity :** 1 sample

**Test Result:**

No.	Sample Name	Sulfate Ash, mass % (%RSD)
1	Mix-CPOME	0.0050 (0.0004)

Limit of the method 0.005 mass %

(Ms. Patchara Sukonrat)

Inspector

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**Figure E.9** Sulphur ash content of biodiesel made from MCPO



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No. 1105/50 Page 1/1

**TEST REPORT**

**Client Name and Address :** Mr. Surachai Jansri  
Department of Mechanical Engineering, Faculty of Engineering, PSU.

**Test Request Form No.:** 1223/50 (Refer : F-ASO-022 No. 1148/50 Date; April 30, 2007)

**Test item(s) received date :** May 9, 2007

**Analyst :** Ms. Wachiraporn Thongbun

**Test performed date :** May 2, 2007

**Test Method used :** Refer to REF-RES-ASTM D 2709-96

**Test Instrument :** Centrifuge (Koehler Benchmark 2000)

**Test Technique:** Centrifuge

**Test Condition :** Relative centrifuge force (rcf)  $800 \pm 60$

**Test item(s) description :** Biodiesel (B100) **Quantity :** 1 sample

**Test Result :**

No.	Sample	Volumetric percent of water and sediment
1	Mix-CPOME	<0.05%

*Patchara Sukonrat*

(Ms. Patchara Sukonrat)

Inspector

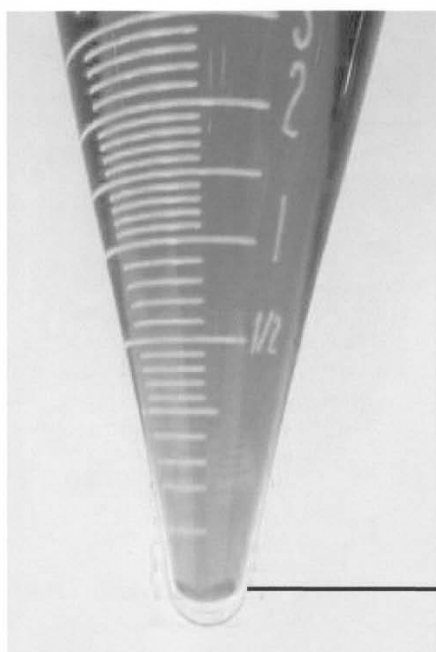
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**Figure E.10.1** Water and sediment in biodiesel obtained from MCPO

Attachment data of sample (Refer: F-ASO-022 No. 1148/50)

- Mix-CPOME



Water and sediment

**Figure E.10.2** Water and sediment in biodiesel obtained from MCPO



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No.1076/50 Page 1/1

TEST REPORT

**Client Name and Address :** Mr. Surachai Jansri  
Department of Mechanical Engineering, Faculty of Engineering, PSU.

**Test Request Form No.:** 1224/50

**Test item(s) received date :** May 9, 2007 (refer to F-ASO-022 No. 1150/50 date April 30, 2007)

**Analyst :** Miss Songsuda Promthong

**Test performed date :** May 2, 2007

**Test Method used :** In house method refer to ASTM D664-01

**Test Instrument :** 794 Basic Titrimo (Potentiometric Autotitrator)

**Test Technique:** Potentiometric Titration

**Test Condition :** -

**Test item(s) description :** Biodeisel (B100) **Quantity :** 1 Sample

**Test Results :**

No.	Sample Name	Acid Number (mgKOH/g)	%RSD
1	Mix - CPOME	0.25	1.22

\* The result is referred to folder 1150-50

(Ms.Patchara Sukonrat)

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Figure E.11 Acid number of biodiesel made from MCPO



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## TEST REPORT

**Client Name and Address :** Mr. Surachai Jansri  
 Department of Mechanical Engineering, Faculty of Engineering,  
 Prince of Songkla University.

**Test Request Form No.:** 1147/50

**Test item(s) received date :** April 30, 2007

**Analyst :** Miss Sathida Malee

**Test performed date :** May 13, 2007

**Test Method used :** Refer to EN 14105:2003

**Test Instrument :** HP 6890 Gas Chromatograph with Flame Ionization Detector

**Test Technique:** Gas Chromatography

**Test Condition :** Inlet temperature: Track oven                      Detector temperature: 380°C  
 Oven initial temperature: 50°C, hold 1 minute  
 Ramp to : 180 ° C , at 15°C / minute  
 Ramp to : 230 ° C , at 7 ° C / minute  
 Ramp to : 370 ° C , at 10 ° C / minute, hold 5 minutes  
 Column: Select Biodiesel for Glycerides , length 10 m., 320 µm I.D, 0.1 µm film thickness plus  
 Retention gap, length 2 m., 530 µm I.D

**Test item(s) description :** Biodiesel (B100)                      **Quantity :** 1 Sample

**Test Results :**

Sample	Content (%RSD), %				
	Free glycerol	Monoglyceride	Diglyceride	Triglyceride	Total glycerol
Mix_CPOME	ไม่พบ	0.65 (0.37)	0.78 (2.43)	7.55 (1.81)	1.06 (1.13)
Standard criteria	≤ 0.02	≤ 0.80	≤ 0.20	≤ 0.20	≤ 0.25

Refer to Folder 1147\_50

(Miss Patchara Sukonrat)

Inspector

**Remark** This Test report is valid only for the tested sample.

This test report shall not be reproduced except in full, without written approval of the Scientific Equipment Center.

Figure E.12 Free GL, MG, DG, TG, and total GL in biodiesel produced from MCPO

**APPENDIX F**  
**% DATA ERROR MEAN AND STANDARD DEVIATION IN**  
**CATEGORIES OF THE TWO-STAGE PROCESS**  
**FROM MATLAB7 CURVE FITTING TOOL**

**Table F.1** Rate coefficients and reaction orders of esterification from MATLAB7

Conditions for Reducing FFA in MCPO (MeOH: FFA; Temperature) (Molar Ratios; Degree Celsius)	Rate Coefficients and Reaction Orders of Esterification						
	$k_1$ (min <sup>-1</sup> )	a	b	$k_2$ (min <sup>-1</sup> )	c	d	R <sup>2</sup>
4:1;55	1.985	0.982	0.279	0.452	0.190	0.218	0.950
4:1;60	2.804	1.720	0.587	0.444	0.392	0.570	0.964
4:1;65	2.135	0.311	1.667	2.205	0.417	0.138	0.922
10:1;55	0.697	0.592	0.792	1.022	0.001	0.086	0.848
10:1;60	0.837	0.278	0.976	1.259	0.224	0.078	0.916
10:1;65	0.802	0.622	0.973	0.781	0.356	0.291	0.904
16:1;55	1.035	0.123	0.746	10.380	0.376	0.445	0.962
16:1;60	0.826	0.490	0.560	0.172	0.004	0.382	0.927
16:1;65	0.883	0.312	0.502	1.620	0.179	0.315	0.970

**Table F.2** Rate coefficients of transesterification from MATLAB7

Conditions for Producing CPOME (MeOH: TG; Temperature) (Molar Ratios; Degree Celsius)	Rate Coefficients of Transesterification (min <sup>-1</sup> )						
	$k_3$	$k_4$	$k_5$	$k_6$	$k_7$	$k_8$	R <sup>2</sup>
3:1;55	1.977	0.215	1.278	0.755	0.458	0.074	0.970
3:1;60	1.669	0.211	1.359	0.525	0.607	0.065	0.975
3:1;65	1.698	0.282	1.358	0.420	0.612	0.055	0.970
6:1;55	1.454	0.100	1.049	0.141	0.508	0.049	0.979
6:1;60	1.474	0.086	1.197	0.043	0.623	0.011	0.974
6:1;65	1.509	0.098	1.086	0.068	0.558	0.008	0.974
9:1;55	1.487	0.152	1.205	0.072	0.615	0.013	0.976
9:1;60	1.177	0.102	1.002	0.077	0.548	0.008	0.986
9:1;65	1.233	0.217	0.985	0.152	0.591	0.003	0.992

Formula for calculating mean and standard deviation in categories (Exell, 2005)

Suppose a population of  $n$  measurements  $x_{i,j}$  is divided into  $m$  categories of  $m$  categories of sizes  $n_i$  having mean  $\mu_i$  and standard deviation  $\sigma_i$ , where  $i=1,\dots,m$ , as follows:

$$\mu = \frac{x_{i,1} + \dots + x_{i,n_i}}{n_i},$$

$$\sigma = \left[ \frac{(x_{i,1} - \mu_i)^2 + \dots + (x_{i,n_i} - \mu_i)^2}{n_i} \right]^{\frac{1}{2}}$$

For all population:

$$n = n_1 + \dots + n_m,$$

$$\mu = \frac{n_1\mu_1 + \dots + n_m\mu_m}{n},$$

$$\sigma = \left[ \frac{n_1\sigma_1^2 + \dots + n_m\sigma_m^2}{n} + \frac{n_1(\mu_1 - \mu)^2 + \dots + n_m(\mu_m - \mu)^2}{n} \right]^{\frac{1}{2}}$$

The first in the last expression for  $\sigma$  is the mean of the category variances, and the second term is the variance of the category mean.



**Table F.3** Comparison between the % data error mean and the standard deviation in categories of the two-stage process between raw data and MATLAB7

<b>Categories of % data error</b>	<b>n</b>	<b><math>\mu</math></b>	<b><math>\sigma</math></b>
<b>Esterification</b> (MeOH: FFA; Temperature) (Molar Ratios; Degree Celsius)			
4:1;55	40	15	14
4:1;60	40	35	41
4:1;65	40	28	33
10:1;55	40	36	36
10:1;60	40	24	26
10:1;65	40	55	113
16:1;55	40	25	43
16:1;60	40	82	168
16:1;65	40	19	27
<b>Transesterification</b> (MeOH: TG; Temperature) (Molar Ratios; Degree Celsius)			
3:1;55	60	454	835
3:1;60	60	272	407
3:1;65	60	395	712
6:1;55	60	144	313
6:1;60	60	98	416
6:1;65	60	184	1,144
9:1;55	60	32	34
9:1;60	60	45	93
9:1;65	60	42	39
<b>Whole population</b>	<b>900</b>	<b>125</b>	<b>467</b>